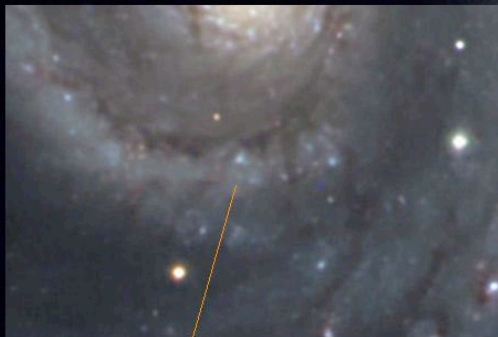


# Supernovae Part 3

## Stellar Core Collapse and Bounce

M. Liebendörfer  
Physics Department  
University of Basel



MAY 8th  
2005

SN2005CS

- Collapse and bounce phases
- Deleptonisation
- Core convergence
- Neutrino luminosities
- Sensitivity to input physics

# Supernova mechanism

for  $1.4 M_{\text{sol}}$ :

Density [g/cm <sup>3</sup> ]	Radius [km]	free fall time scale [s]
$\rho$	$R = \left(\frac{3M}{4\pi\rho}\right)^{\frac{1}{3}}$	$\tau = (6\rho)^{-\frac{1}{2}}$

$10^9$	873	0.123
$10^{10}$	405	0.039
$10^{11}$	188	0.012
$10^{12}$	87	0.004
$10^{13}$	41	$1.2 \times 10^{-3}$
$10^{14}$	19	$0.387 \times 10^{-3}$

- progenitor core that collapses within  $\sim 1$ s: 10'000 km
- this is  $\sim$  up to O-layer

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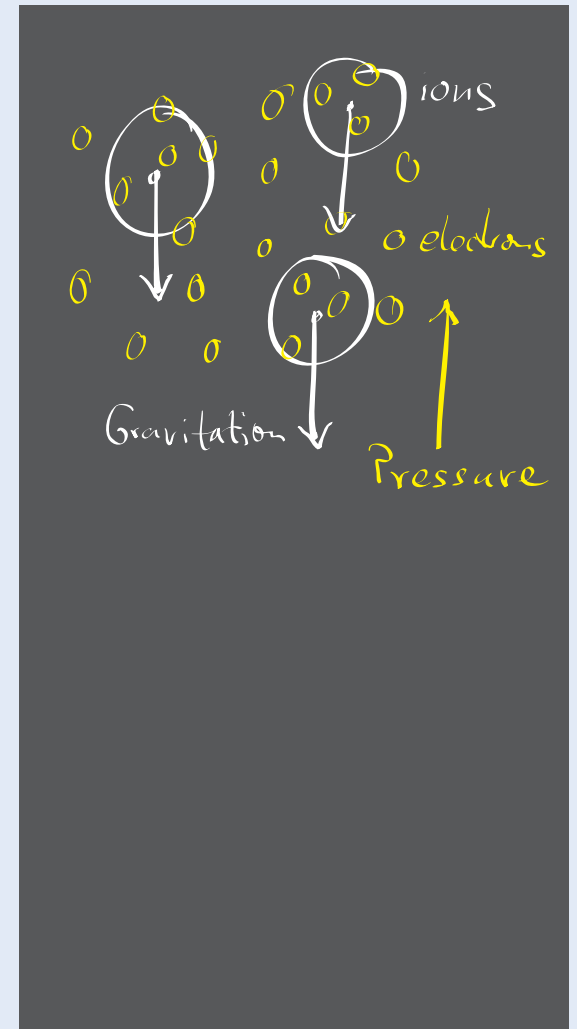
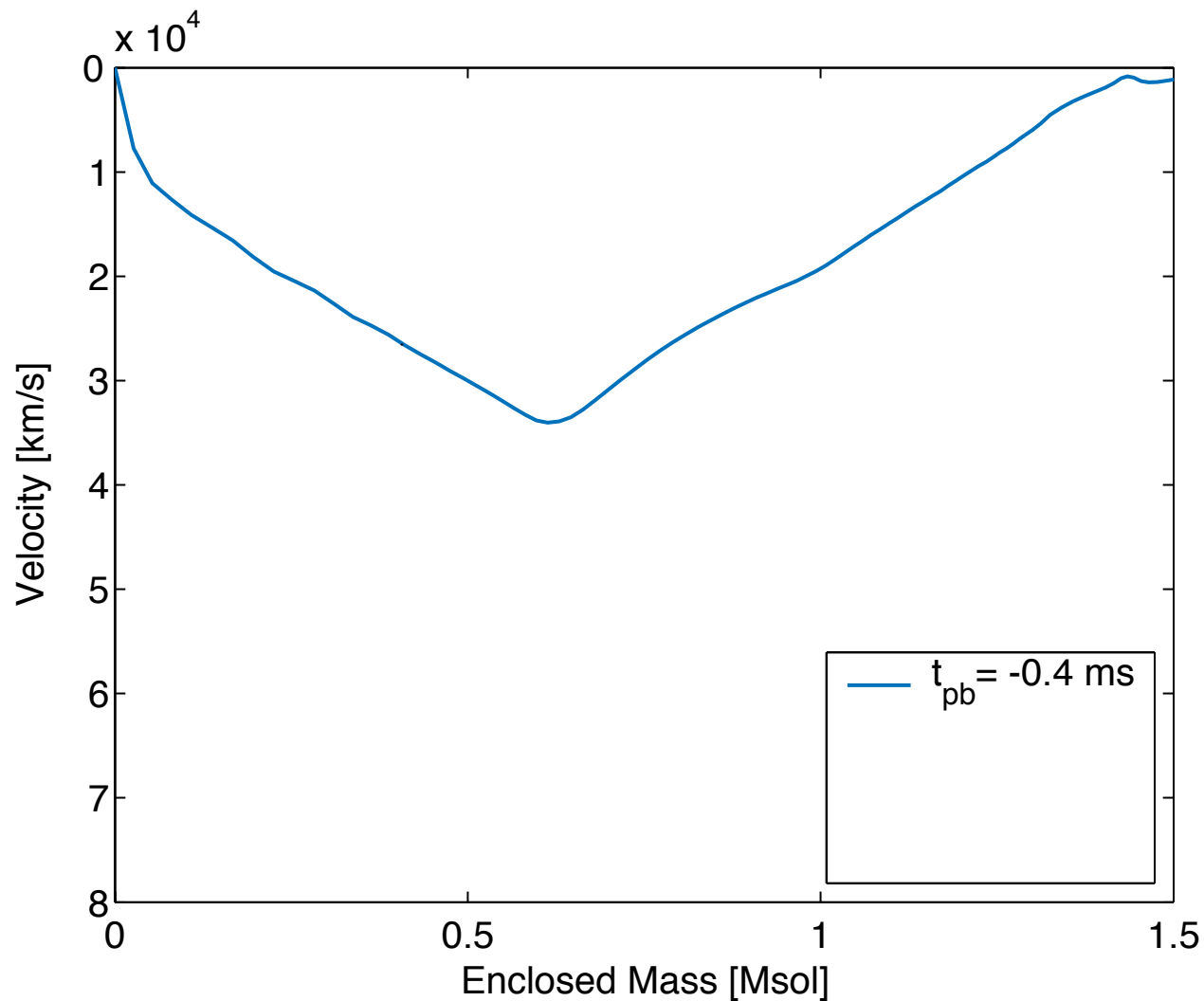
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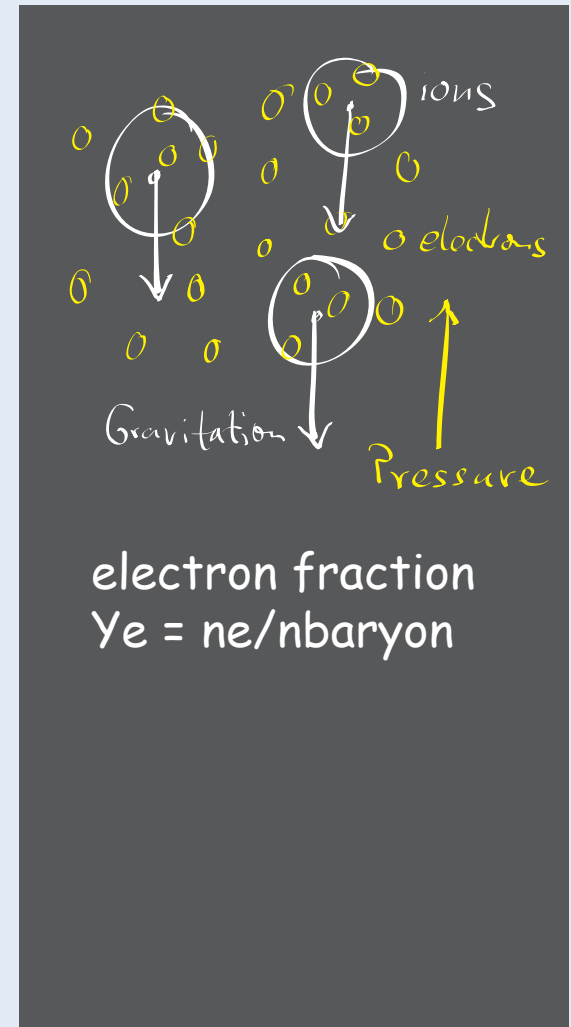
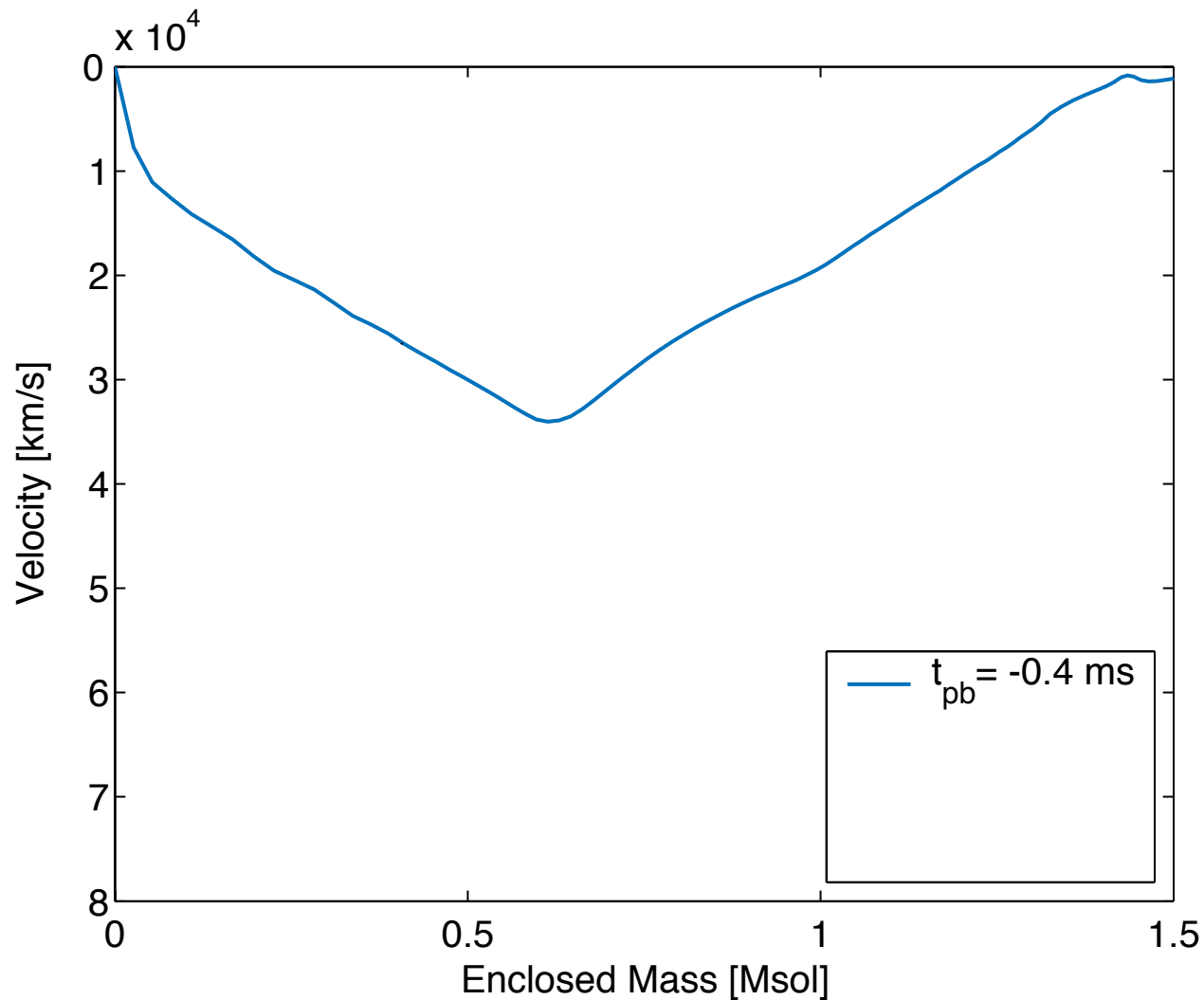
*ν-sphere* (handwritten label between  $10^{12}$  and  $10^{13}$  g/cm<sup>3</sup>)

- progenitor core that collapses within  $\sim 1$  s: 10'000 km
- this is  $\sim$  up to O-layer
- neutrino sphere: location where a neutrino has the probability to make one more interaction before escape
- neutrino transport relevant in compact region

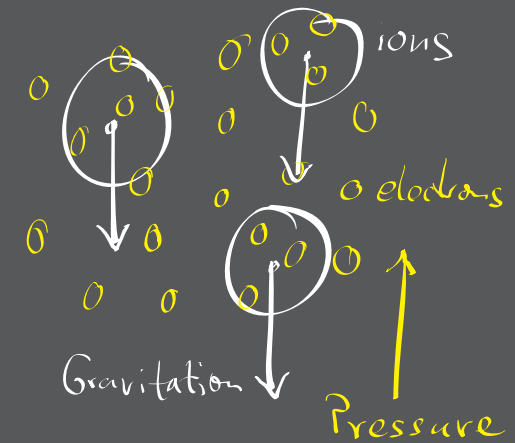
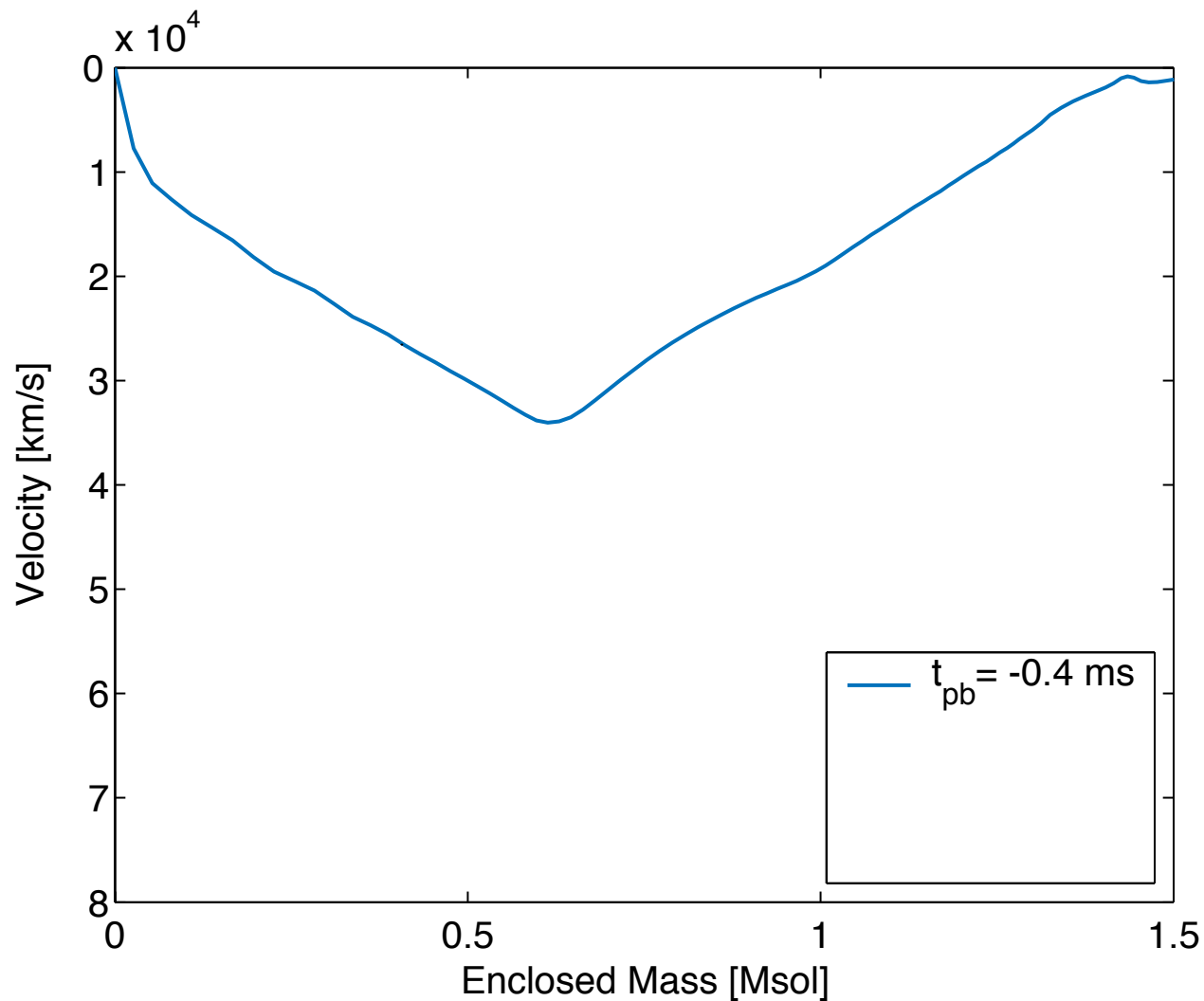
# The collapse phase



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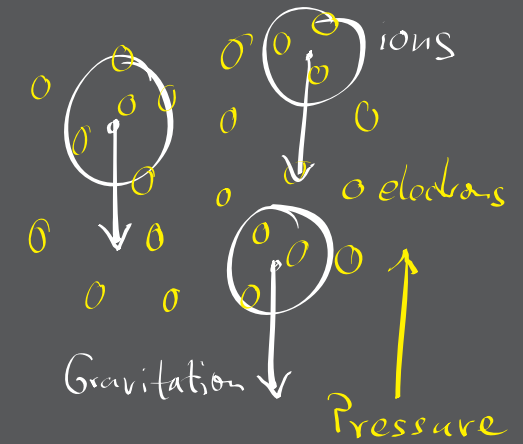
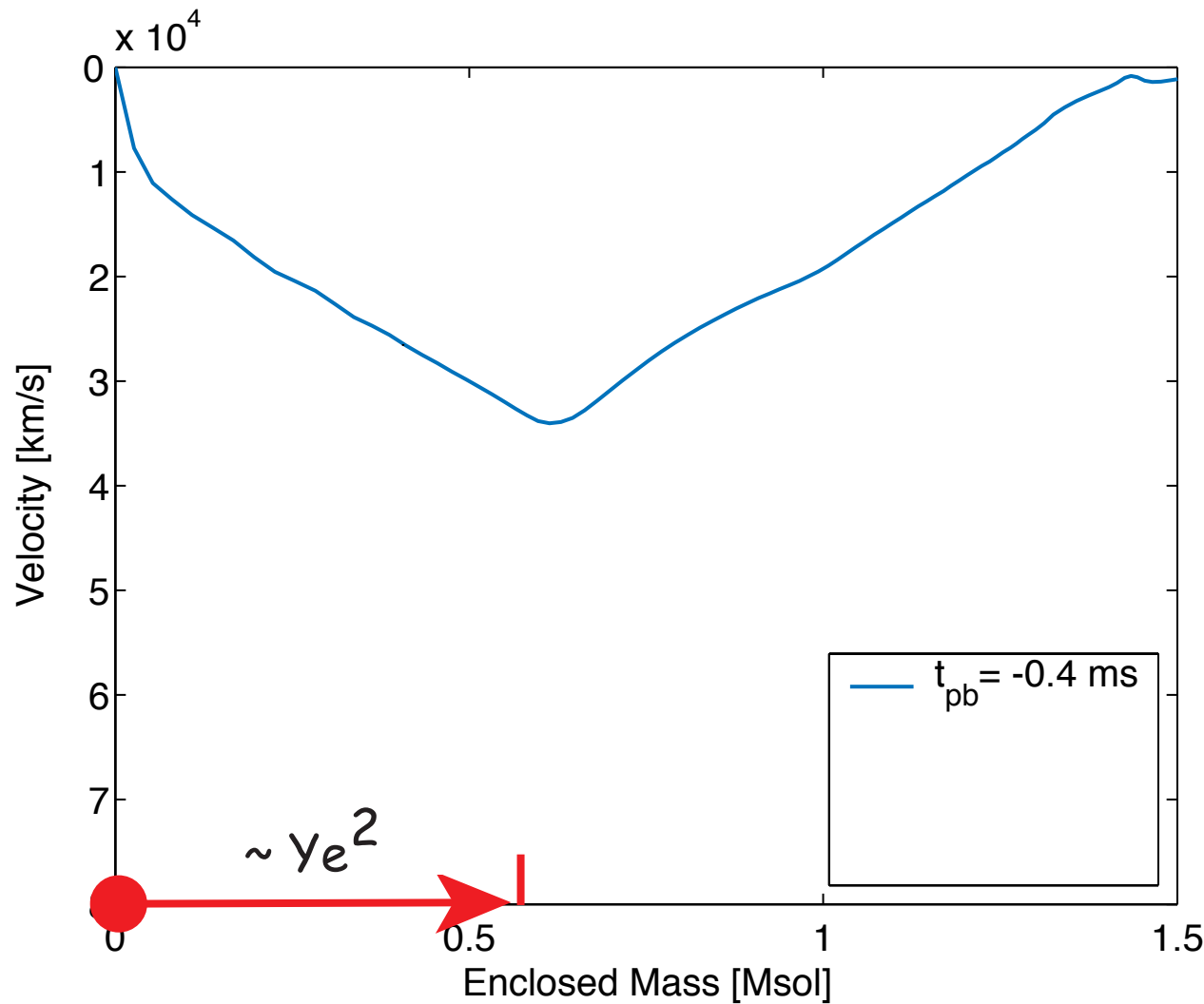
# The collapse phase



electron fraction  
 $Y_e = n_e/n_{\text{baryon}}$

Fermi gas  $p = \mathcal{K} \rho^\gamma$   
 $\mathcal{K} = \frac{\hbar c}{4} (3\pi^2)^{\frac{1}{3}} \left(\frac{Y_e}{m_B}\right)^{\frac{1}{3}}$

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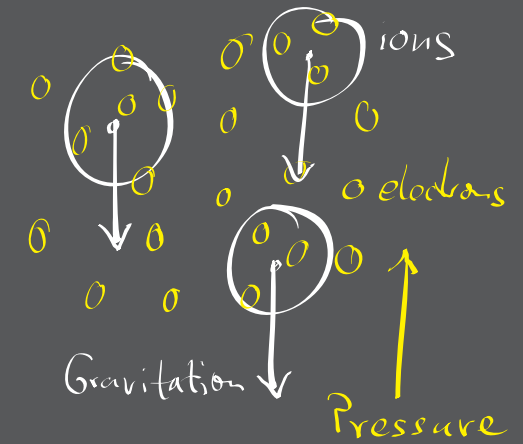
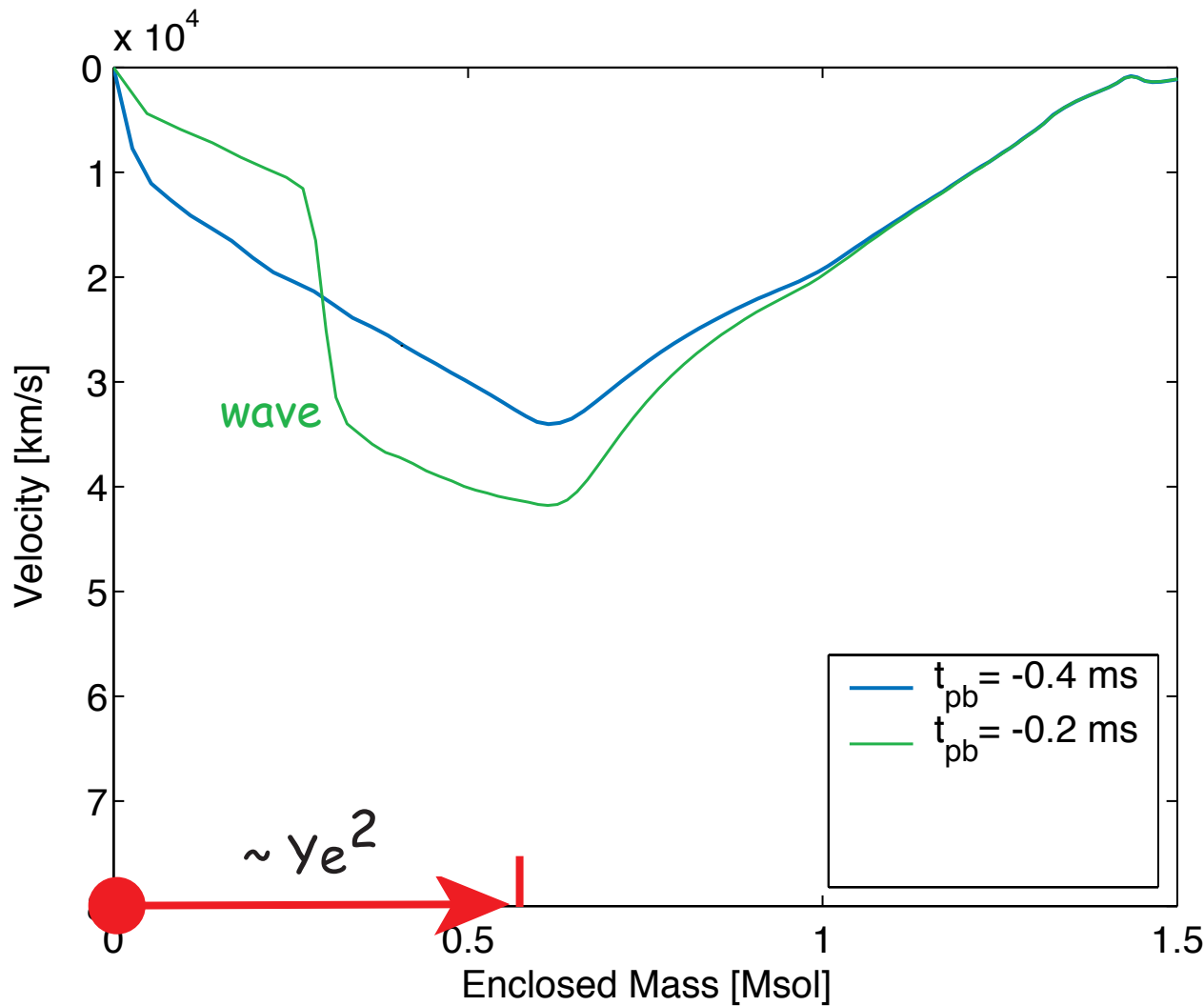
$$\mathcal{K} = \frac{\hbar^2 c}{4} (3\pi^2)^{\frac{1}{3}} \left( \frac{y_e}{m_B} \right)^{\frac{1}{3}}$$

homologous collapse:

$$M_{ic} \simeq (\kappa/\kappa_0)^{3/2} M_0,$$

(Goldreich & Weber 1980)

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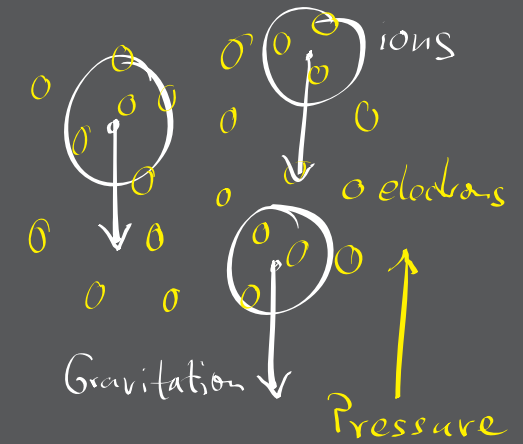
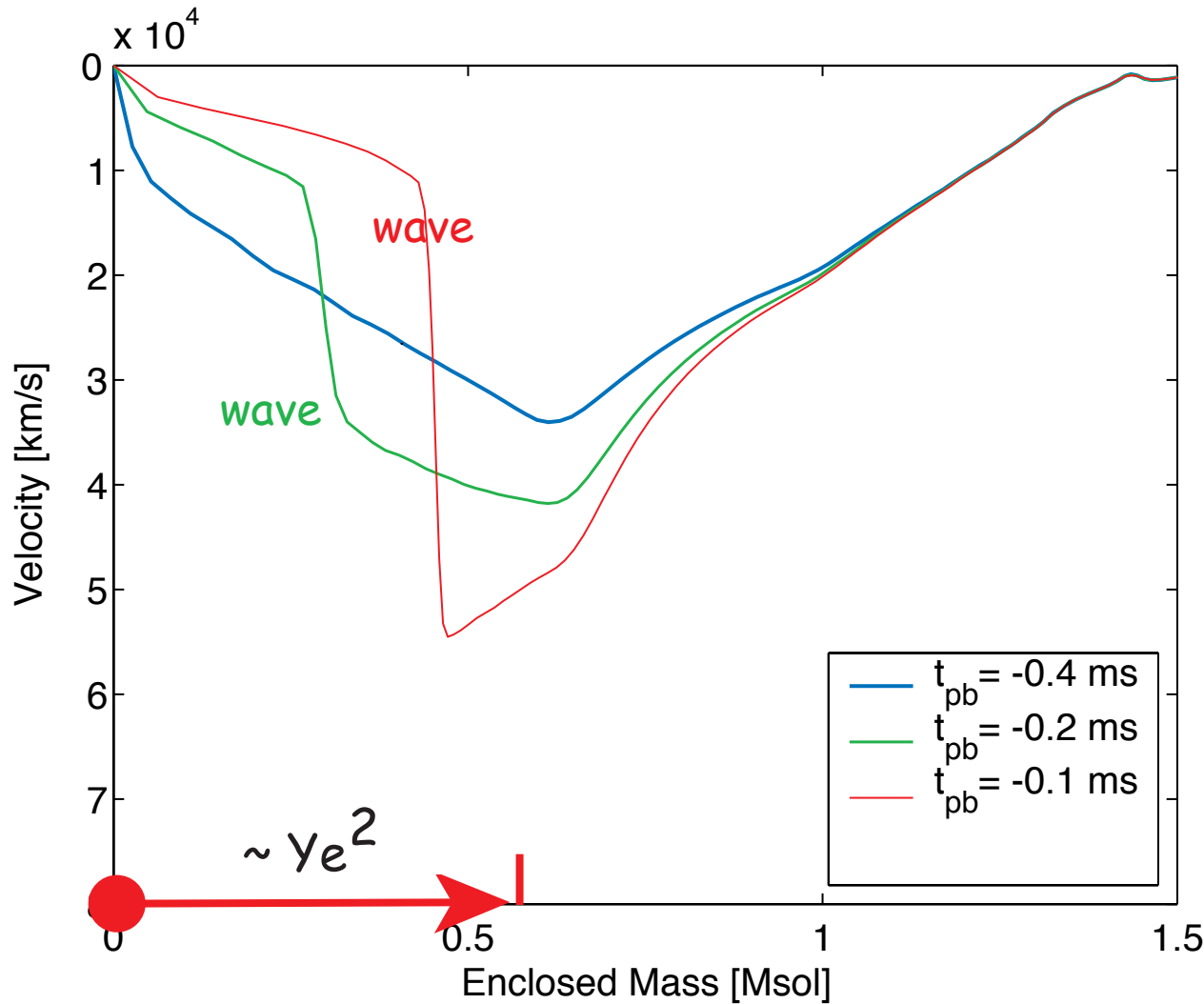
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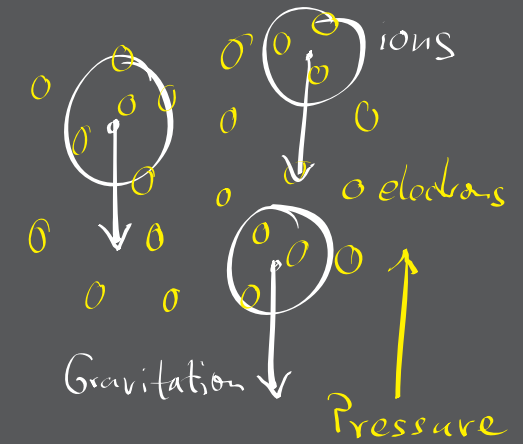
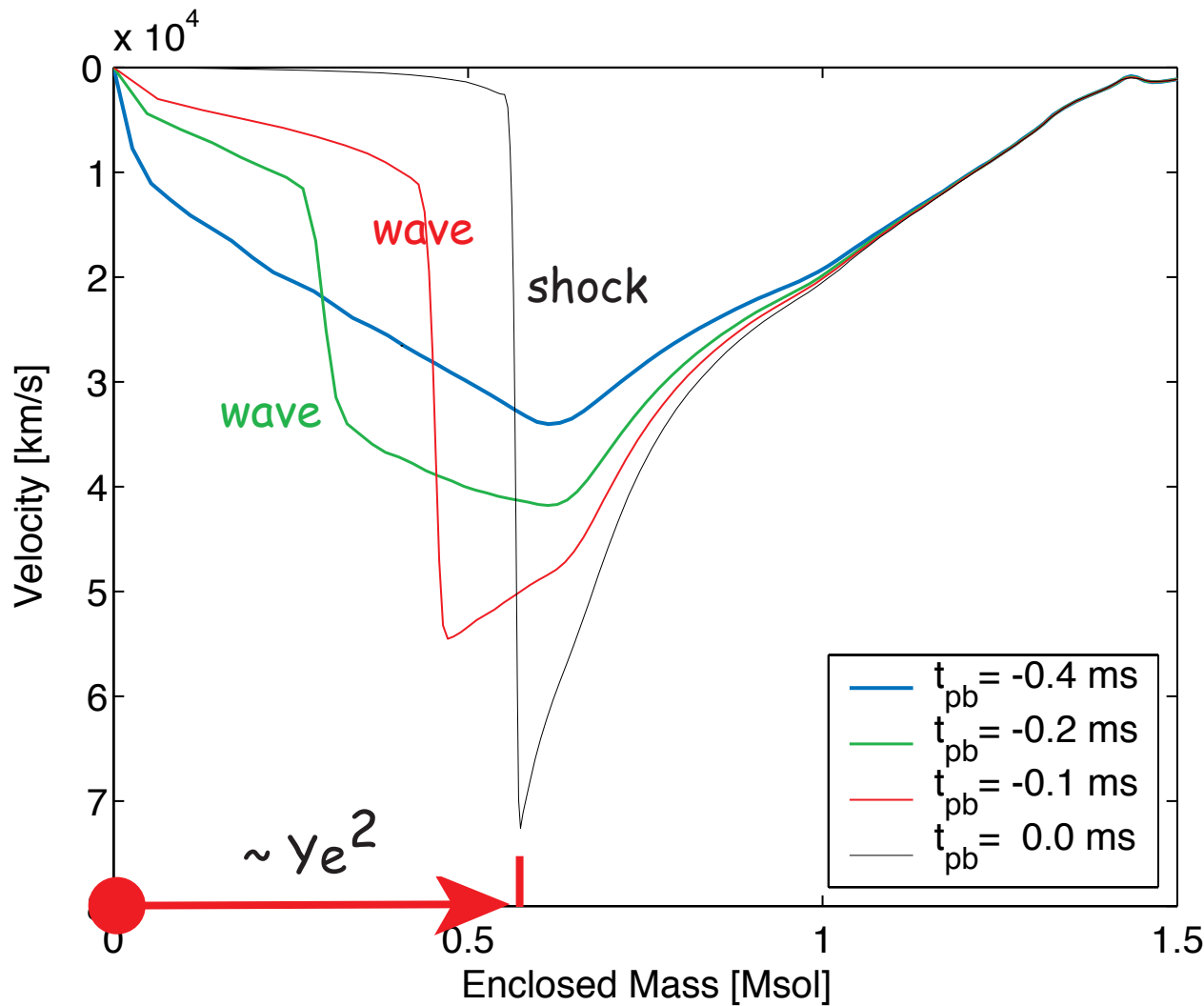
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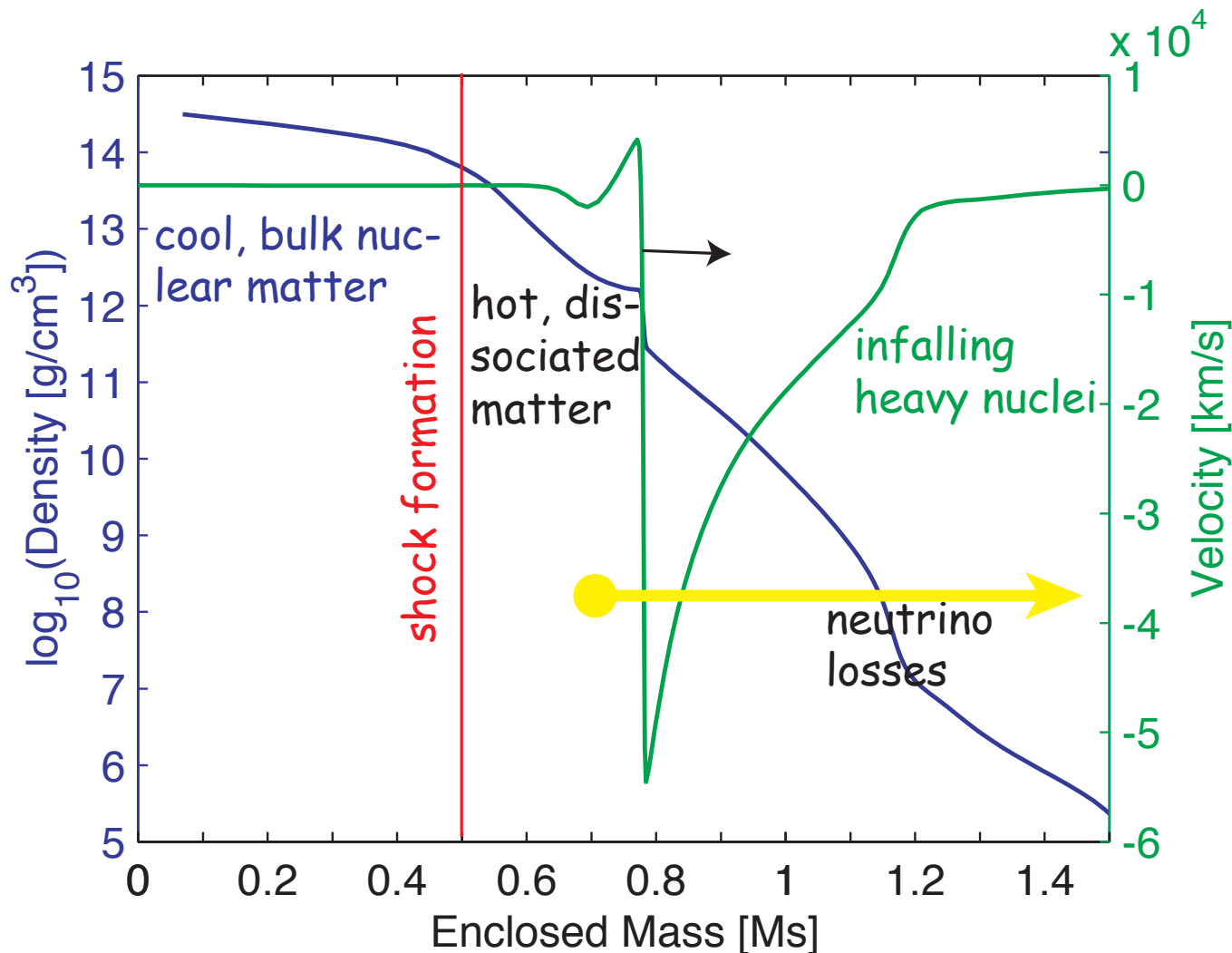
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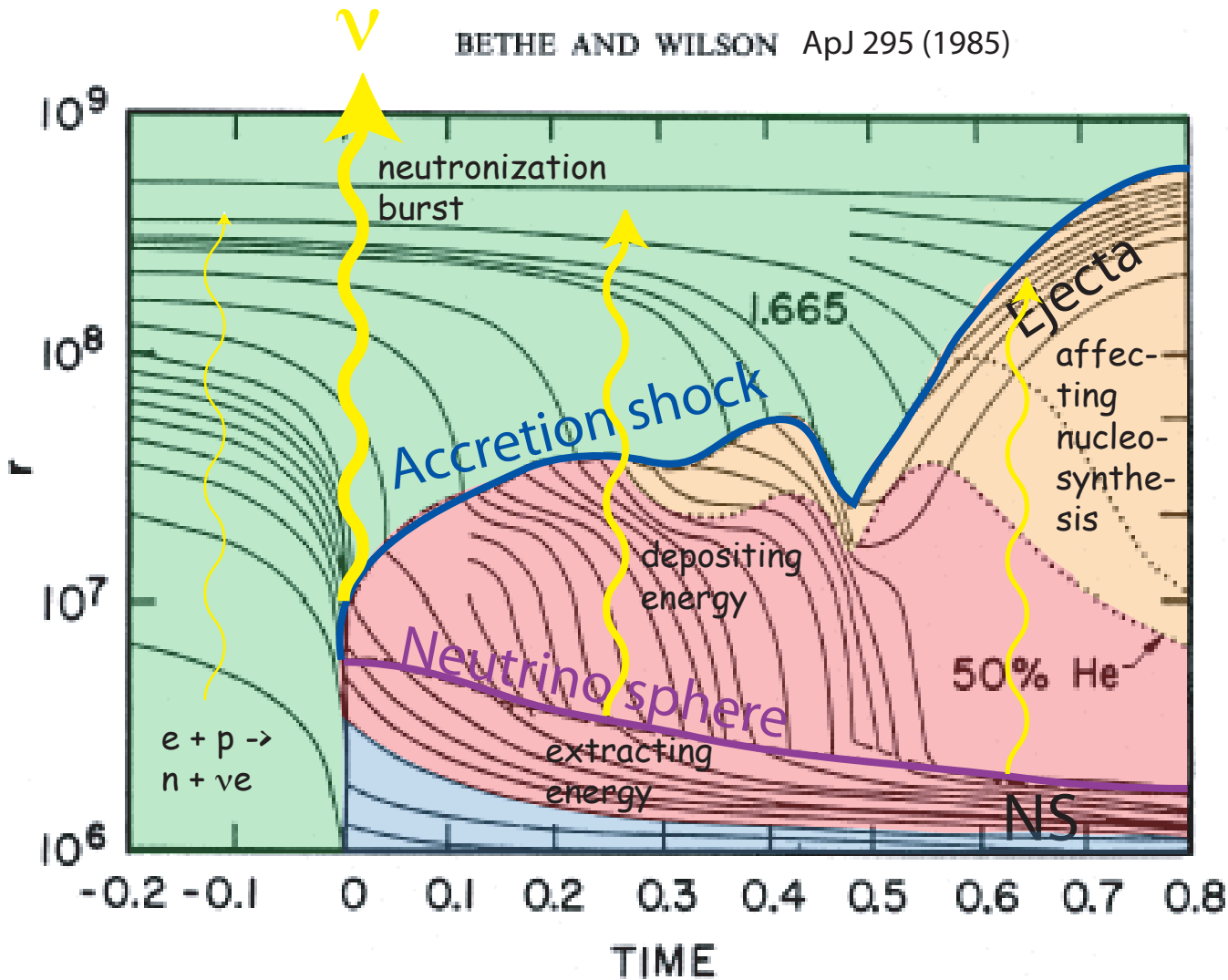
# Bounce: Shock Energy Losses

Within 2-4 milliseconds after bounce:



- dissociation losses and neutrino losses exhaust shock energy
- it was thought that a very strong shock could directly expel outer layers
- cannot be produced in simulations with neutrino transport
- robust result because electron captures on free protons limit uncertainties

# Delayed explosion: 4 phases



collapse phase || postbounce accretion phase | explosion phase  
bounce

Ensemble  
of nuclei

Cool bulk  
nuclear matter

Hot dissociated  
matter

Freeze-out  
of nuclei

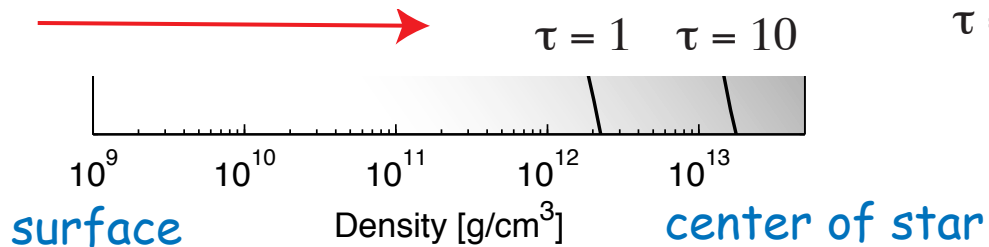
# Deleptonization

Bethe (1990)  
mean free path:

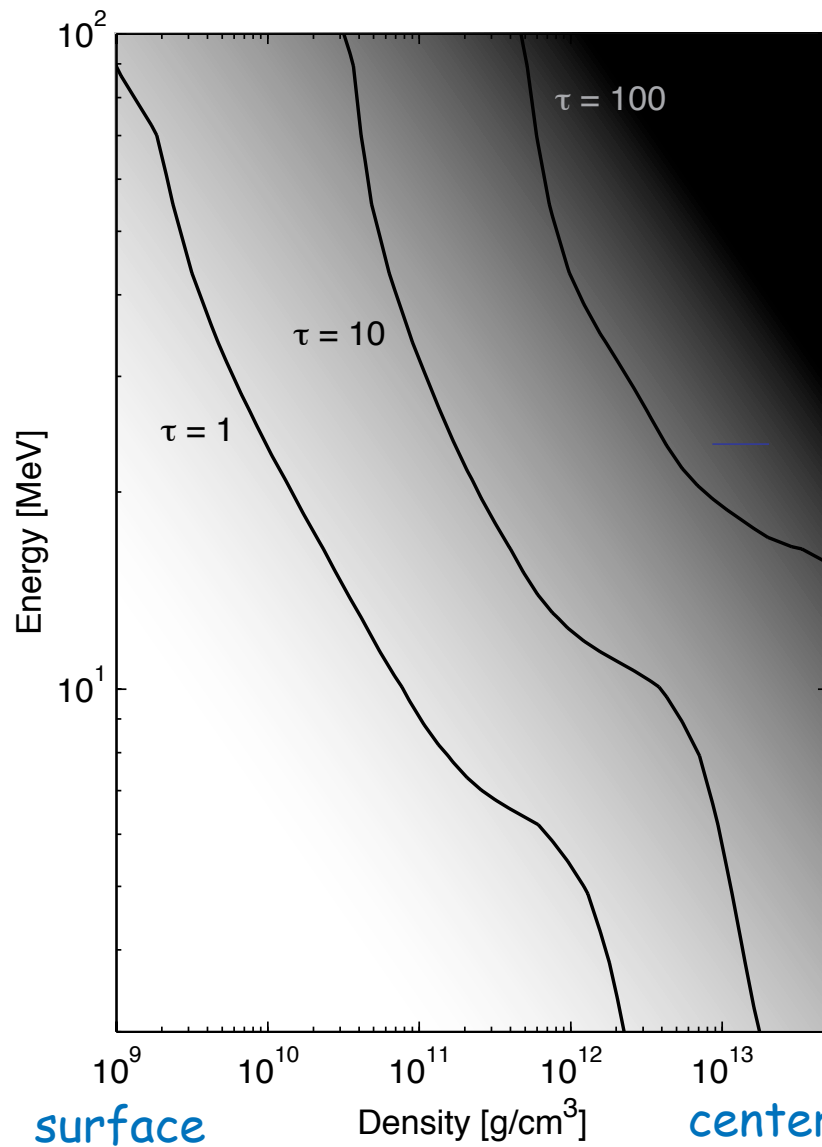
$$\lambda_\nu = 1.0 \times 10^8 \rho_{12}^{-1} [(N^2/6A)X_h + X_n]^{-1} \epsilon_\nu^{-2} \text{ cm} .$$

Optical depth:

$$\tau = \int dr/\lambda$$



# Deleptonization



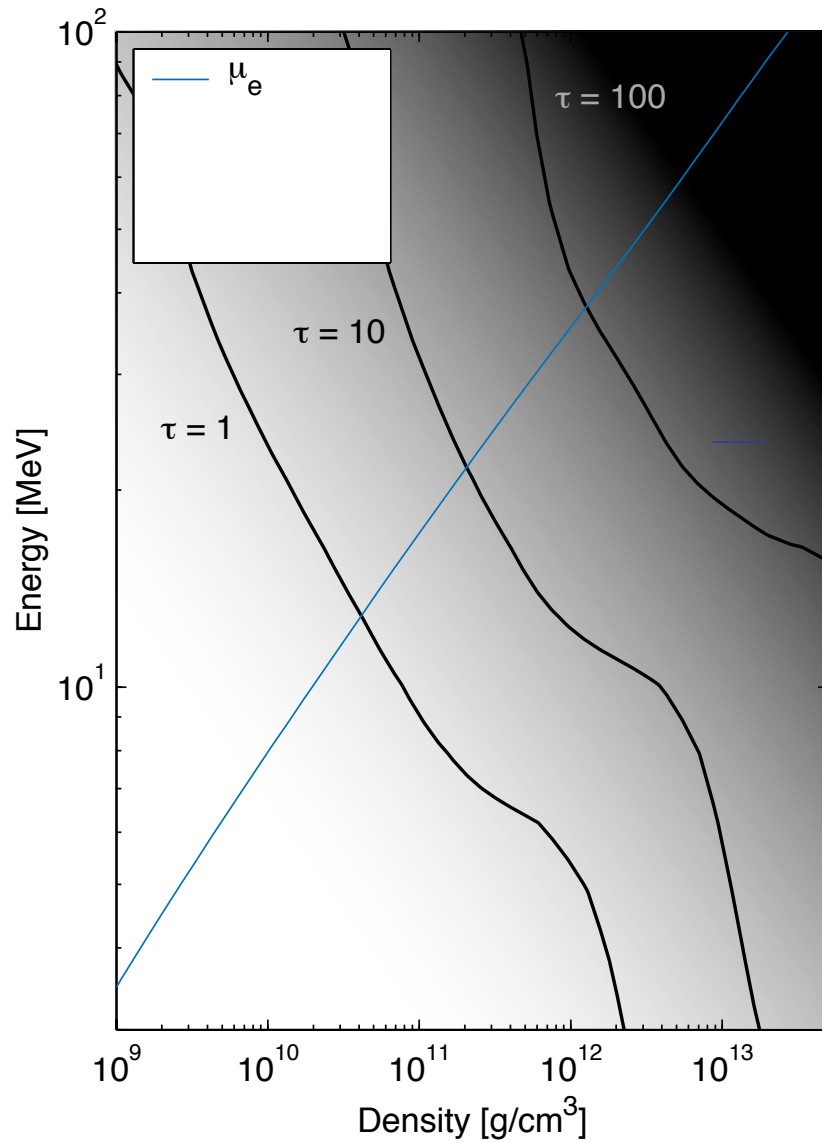
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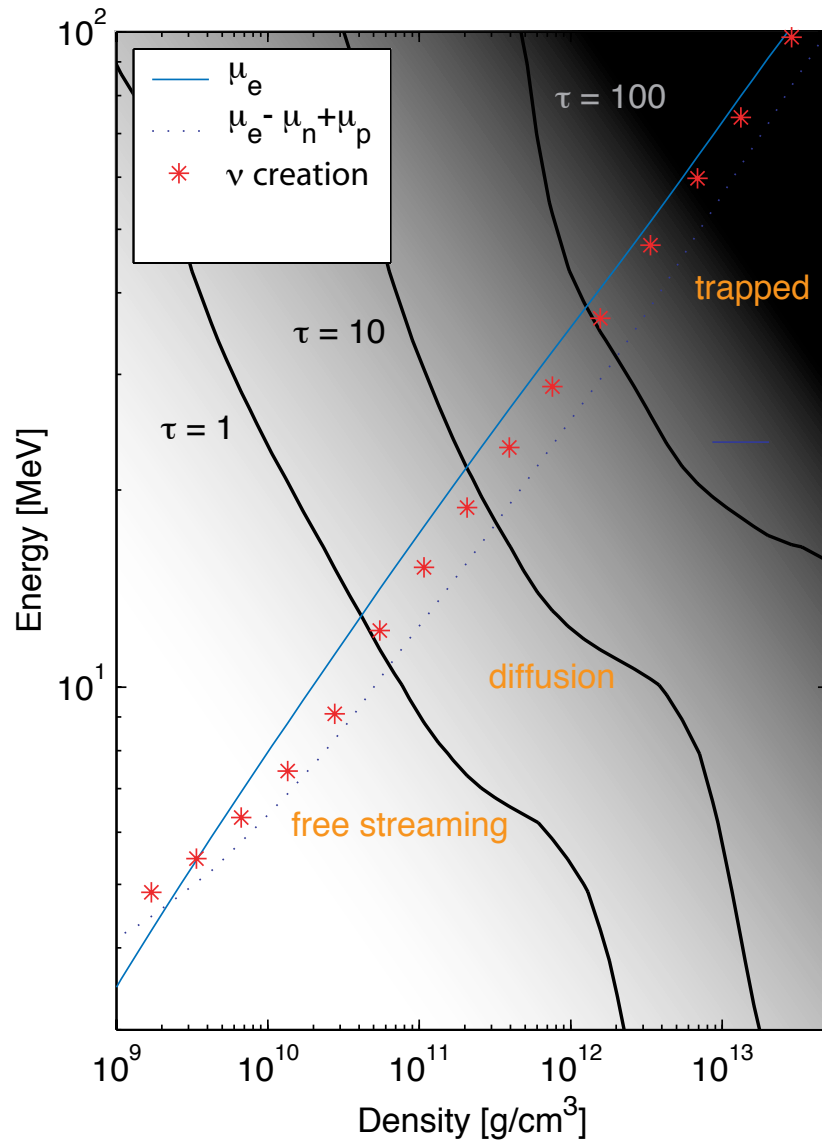
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# Deleptonization



(Martinez-Pinedo, Liebendoerfer, Frekers, 2006)

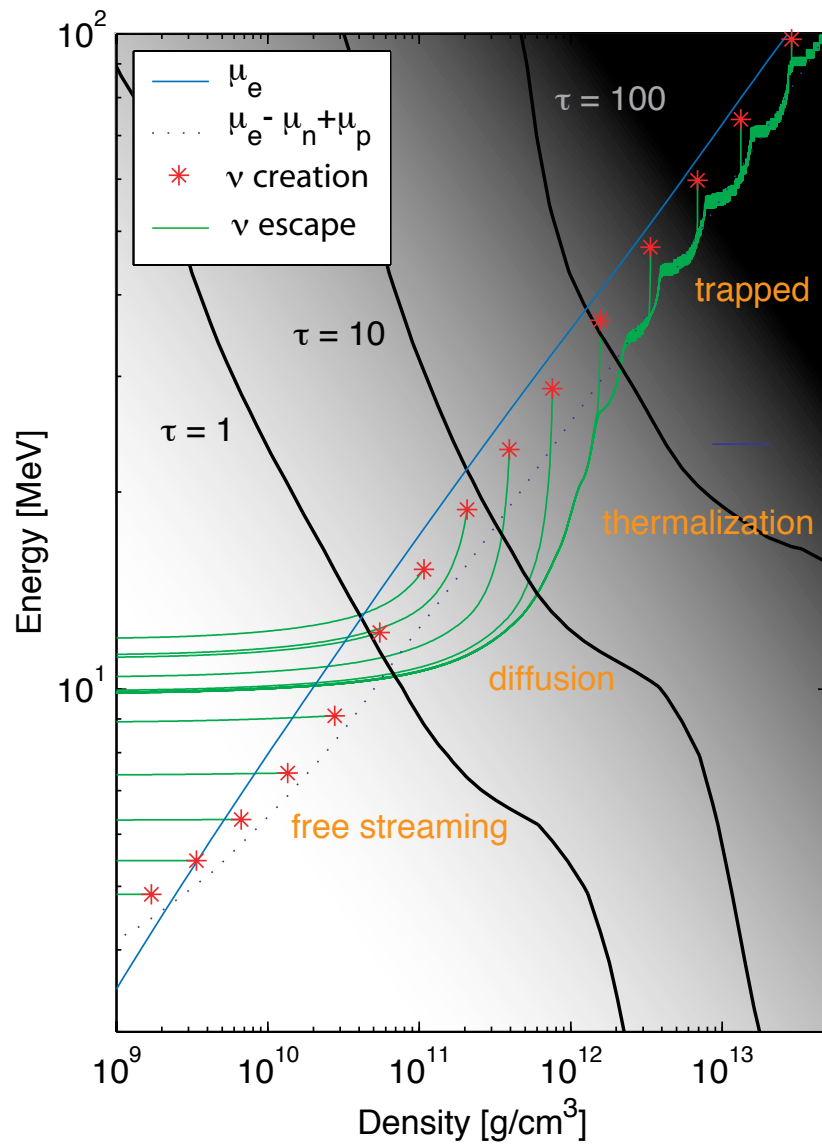
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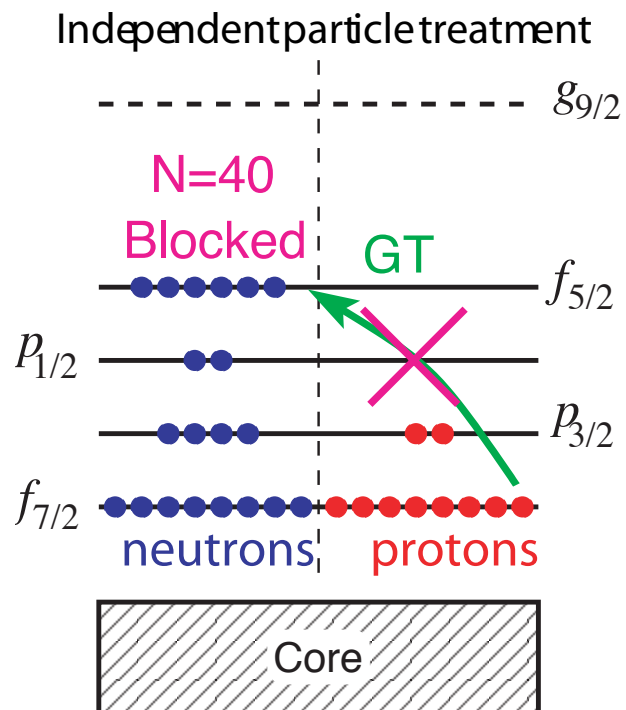


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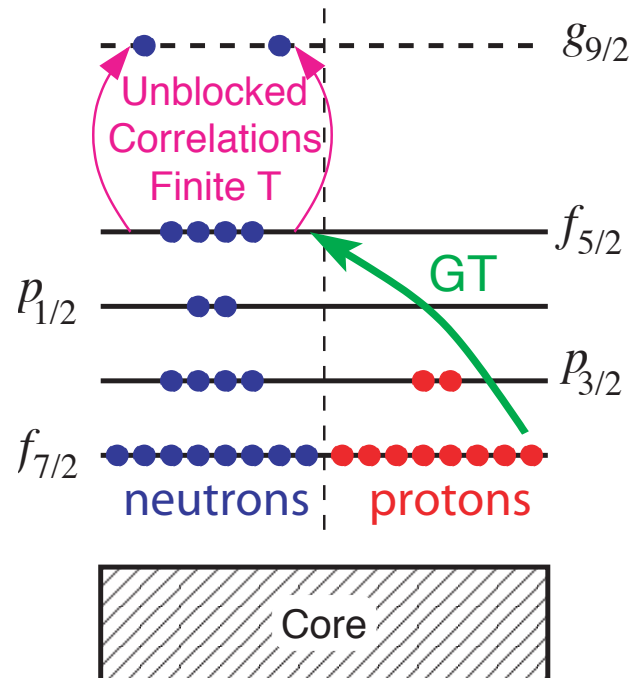
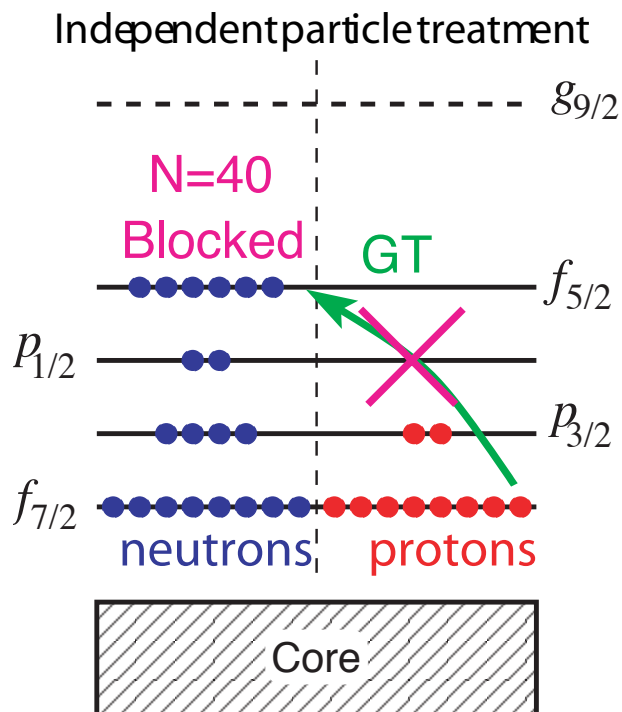
# More neutrinos from electron capture



- Traditional input physics:

Electron capture reactions  
blocked for neutrino-rich  
heavy nuclei

# More neutrinos from electron capture



(Martinez-Pinedo & Langanke 2002)

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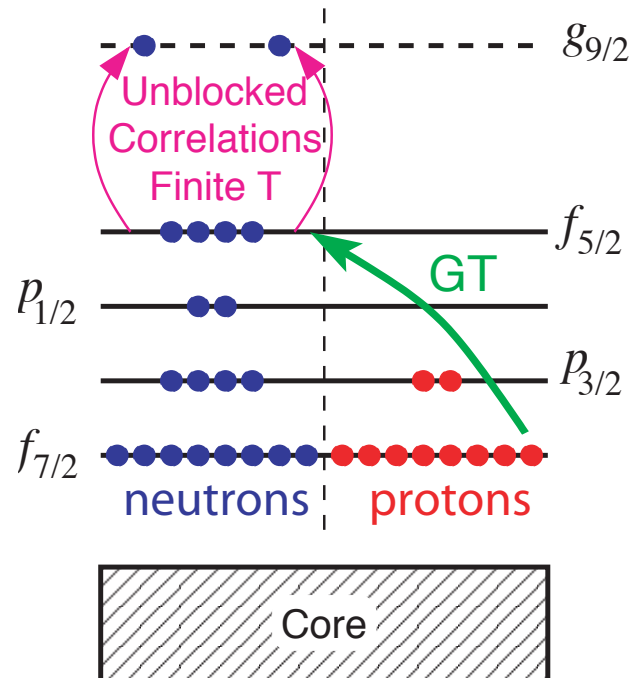
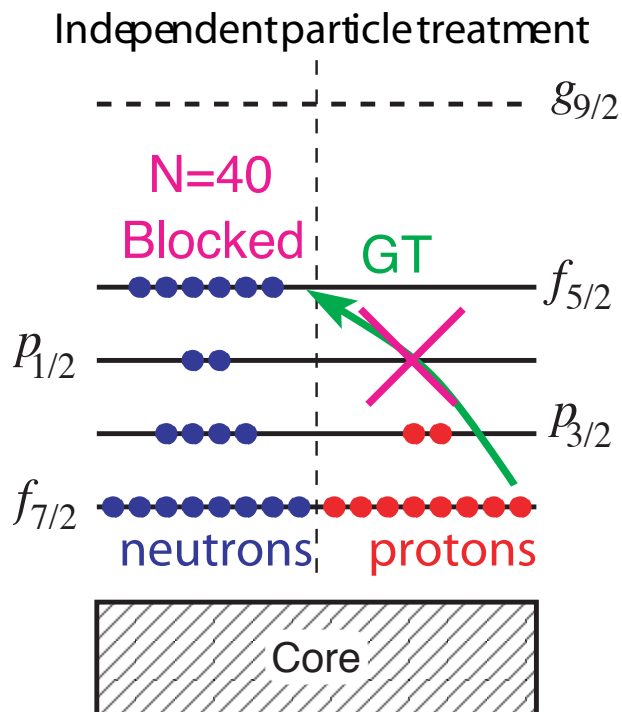
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Electron captures on heavy nuclei proceed and dominate!

(Hix et al. 2003, Marek et al. 2006)

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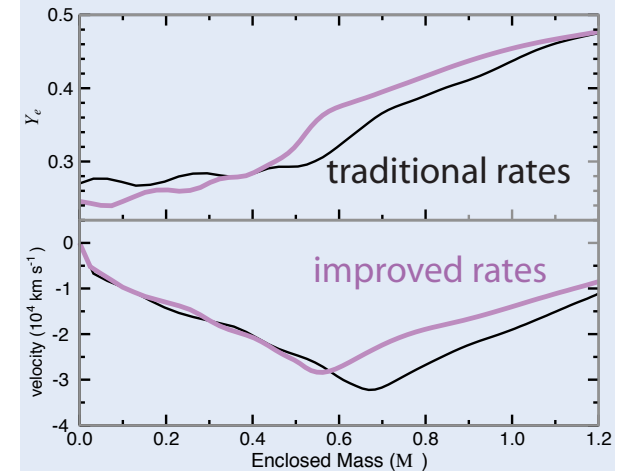
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Electron fraction and velocity profile as function of enclosed mass before bounce

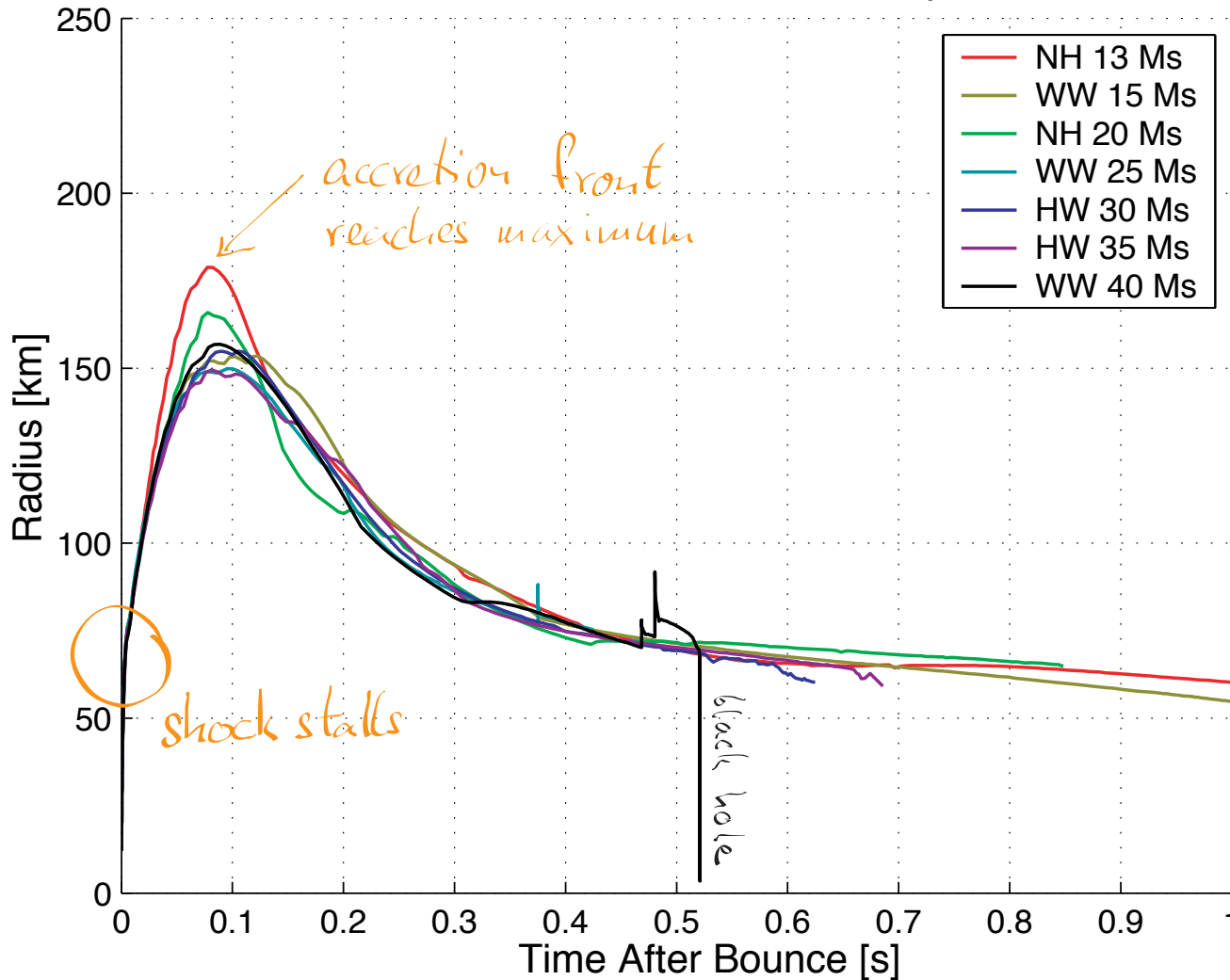


(Langanke et al. 2003)

- the treatment of nuclear structure in n-rich nuclei causes 20% differences in shock formation!

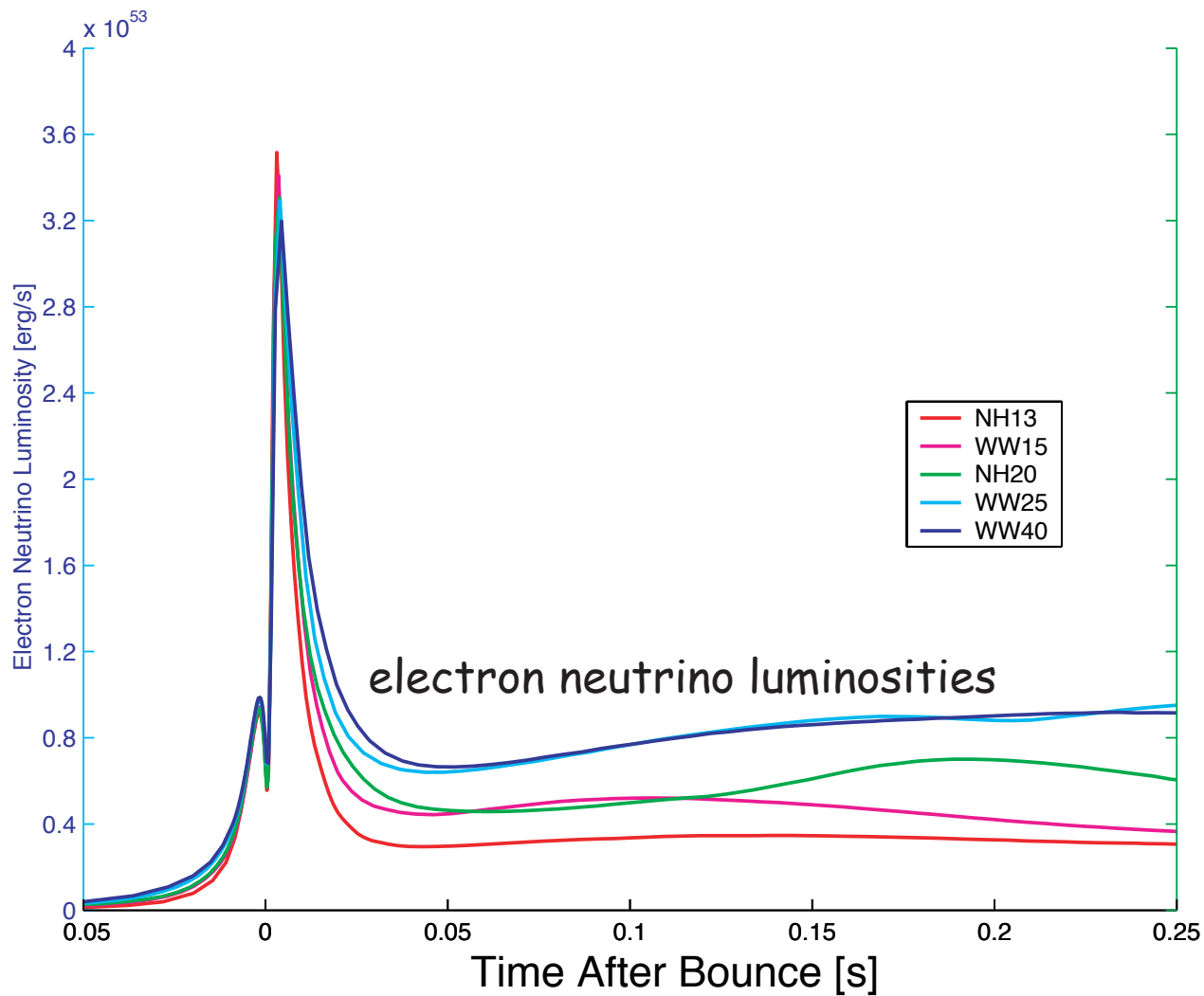
# Modeling: accretion front

General Relativistic Shock Trajectories



- Trajectories of the accretion front for different progenitor stars  $13M_{\text{sol}} < M < 40M_{\text{sol}}$
- calculated with Agile-Boltztran
- 40 Msol model forms a black hole
- 13 Msol model more optimistic
- all other models are VERY similar, why?

# Modeling: neutrino signal



- initially similar luminosities

# Physics: deleptonization

Progenitor 1



Ye - dial

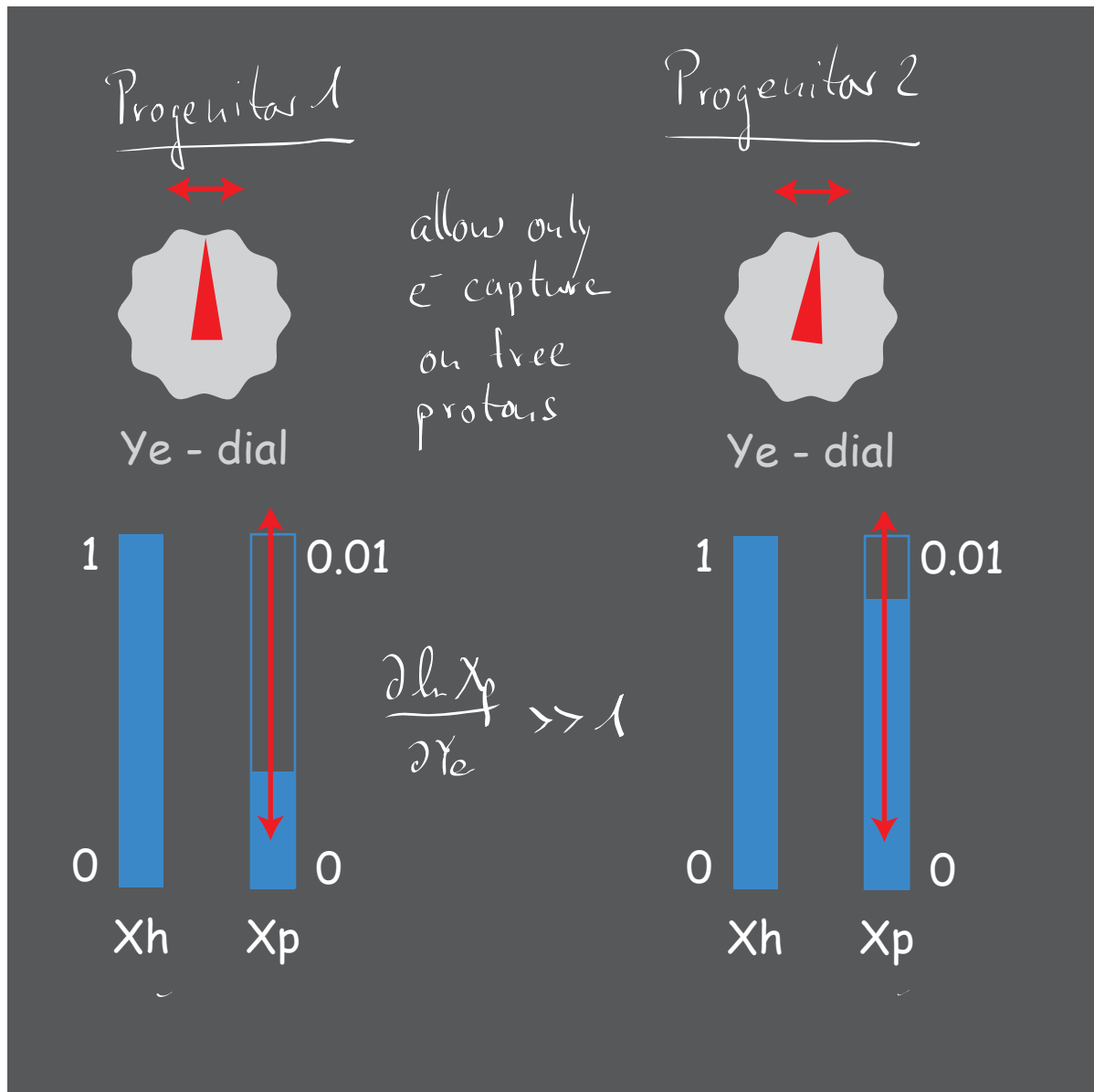
allow only  
 $e^-$  capture  
on free  
protons

Progenitor 2



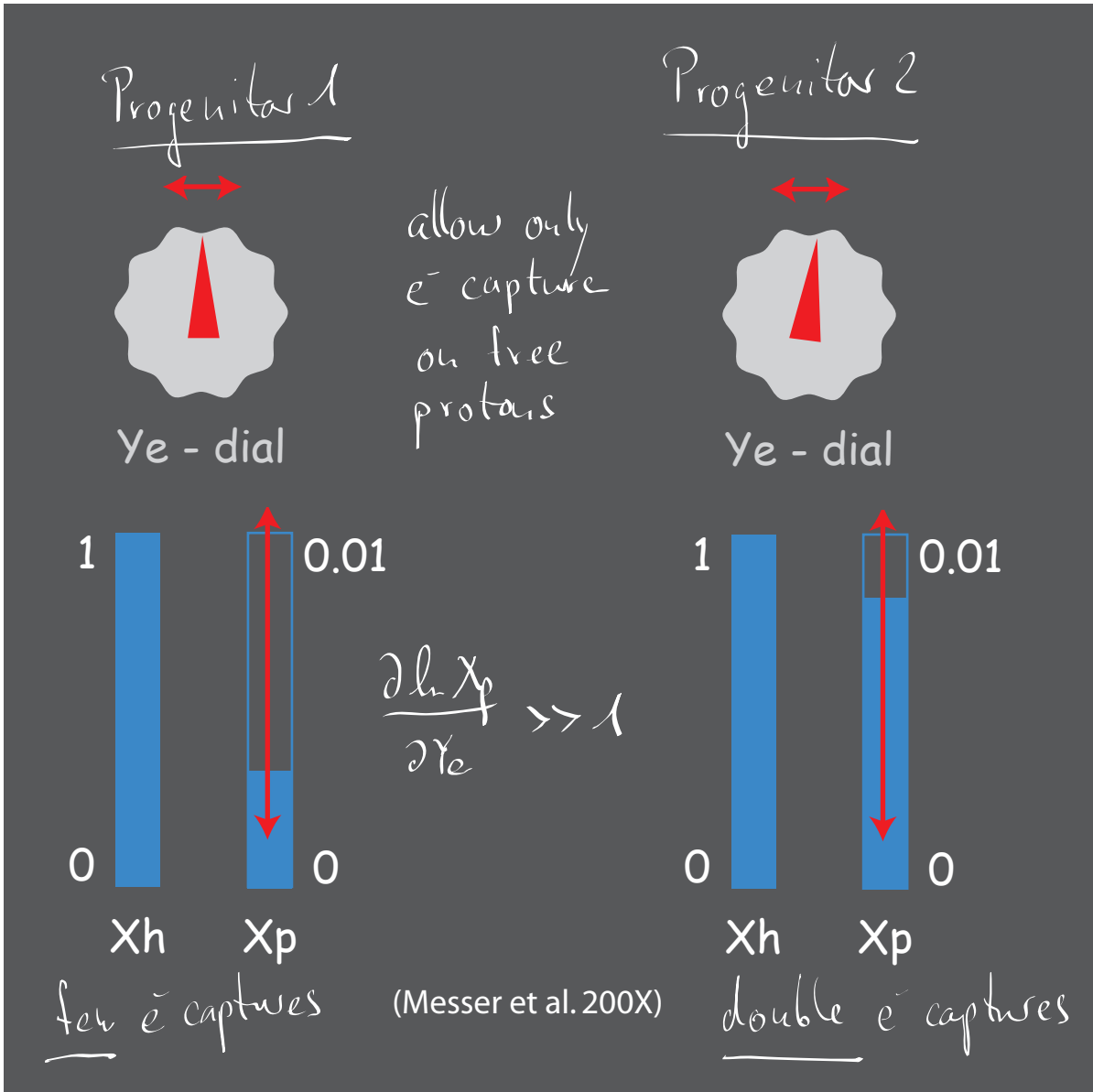
Ye - dial

# Physics: deleptonization

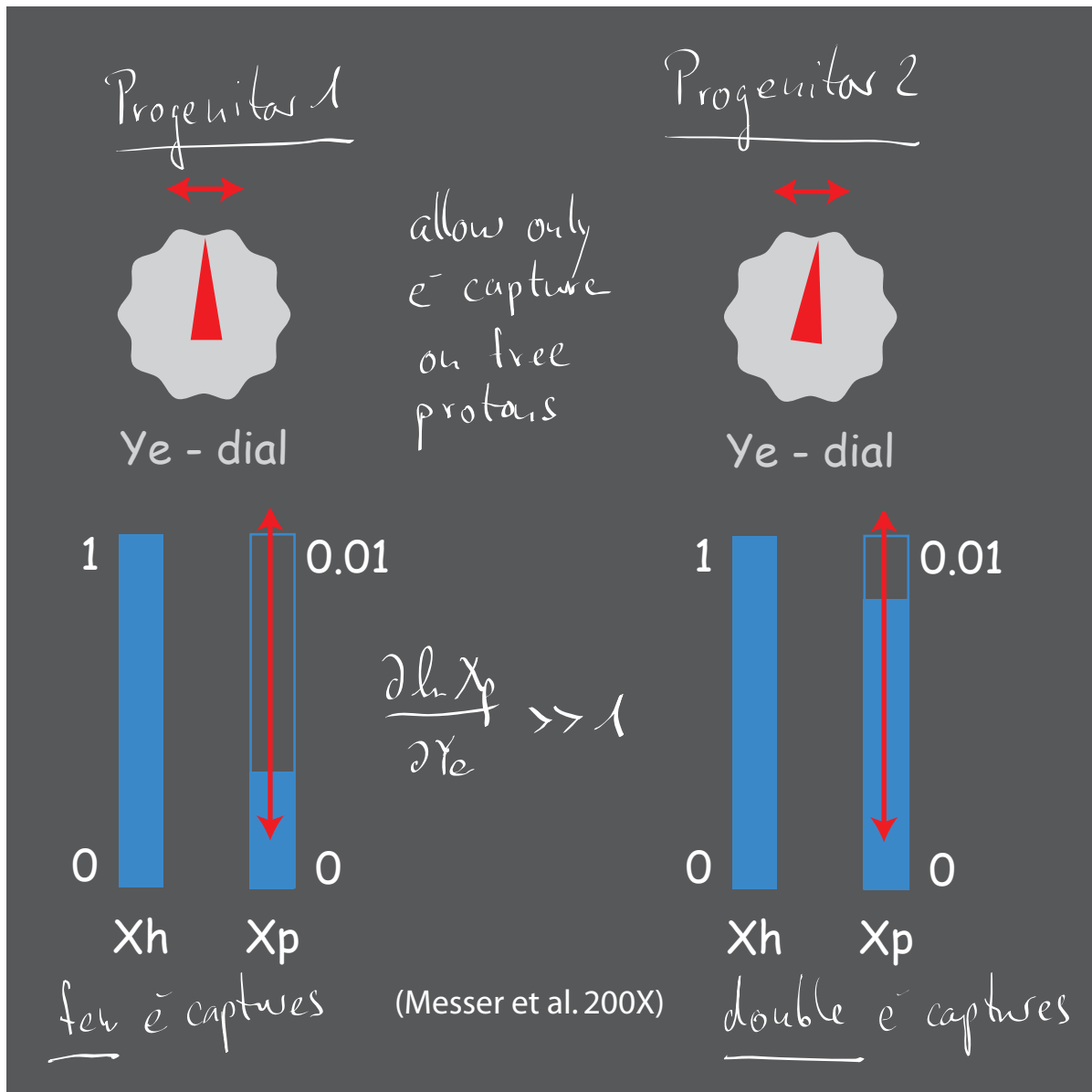




# Physics: deleptonization



# Physics: deleptonization



different progenitors, but:

- approx. same Chandrasekhar mass at onset of collapse
  - upper limit of  $Ye$  by  $e^-$  capture on free protons
  - converging deleptonization
  - same bounce density
- => same bounce dynamics!

# Why no explosion?

Iron core:  $1.2 - 1.4 M_{\odot}$

Inner core at bounce:  $0.45 - 0.65 M_{\odot}$

(Langanke et al. 2003  
Hix et al. 2003)

↑  
best

↑  
very  
optimistic

1) deleptonization

2) dissociation

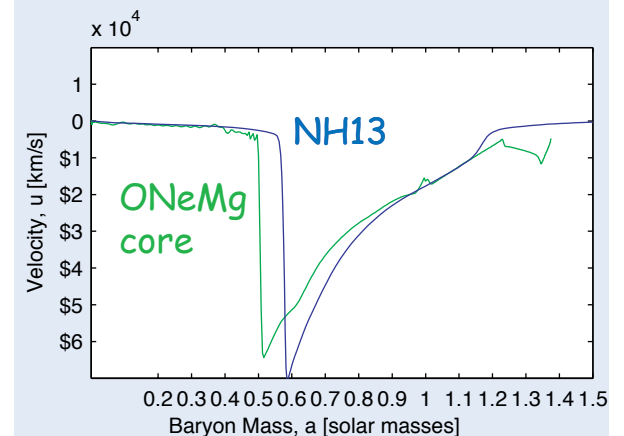
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Rampp & Janka 2000: 15 Msol

Liebendörfer et al. 2001: 13 Msol

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8 MeV/nucleon binding energy

→  $\sim 10^{51}$  erg per  $0.1 M_{\odot}$  dissociation

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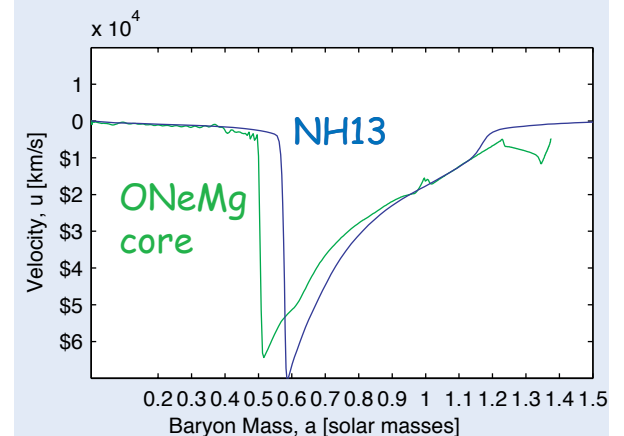
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hydrodynamic shock must stall  
unless input physics is dramatically  
different.

1) deleptonization

2) dissociation

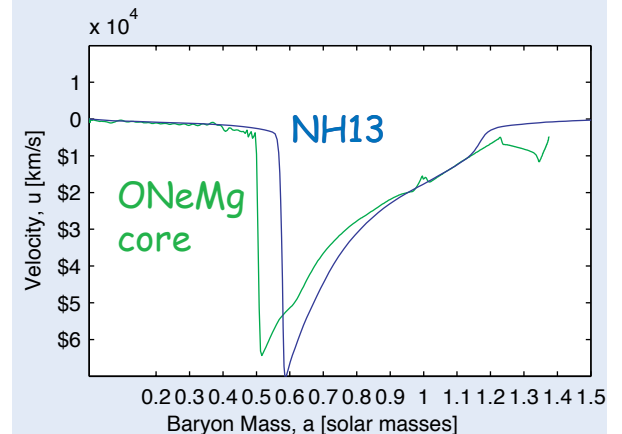
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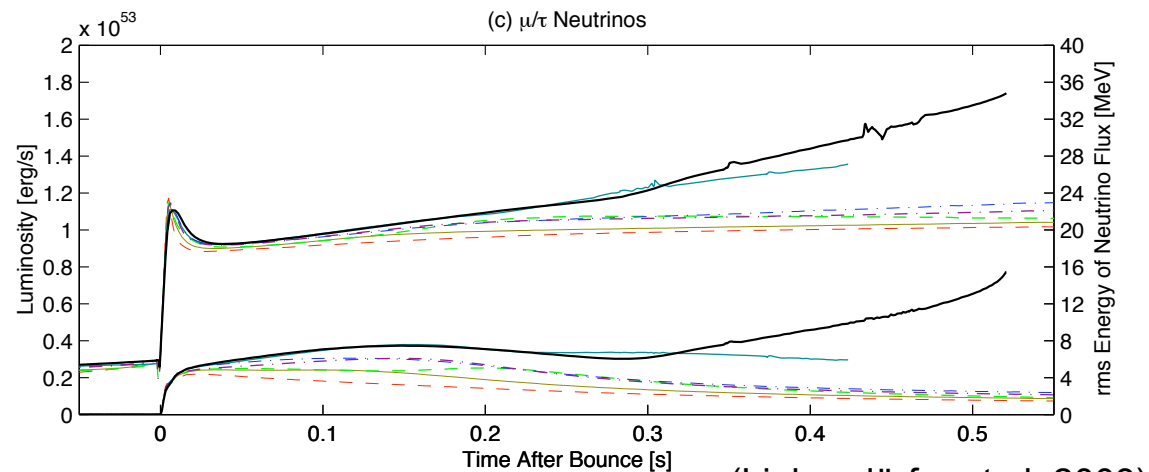
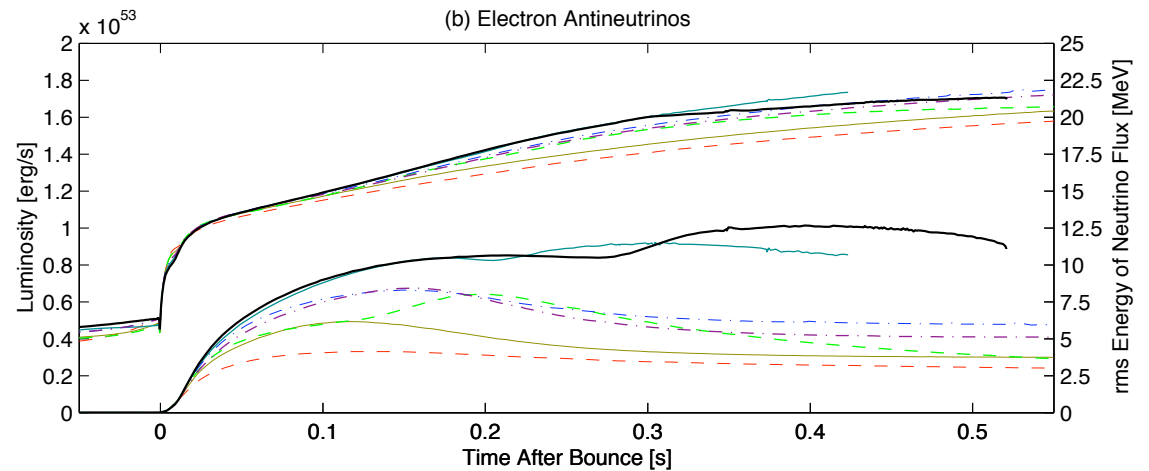
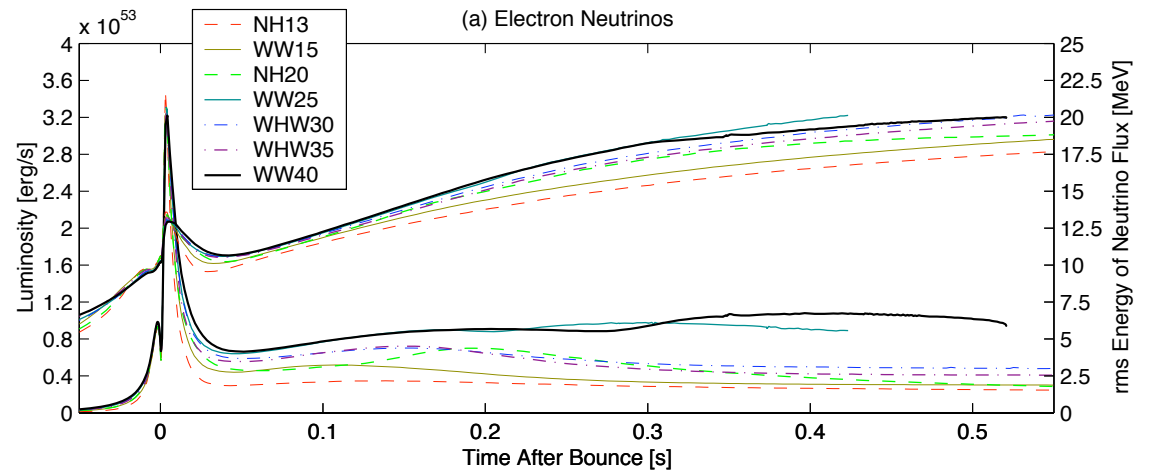
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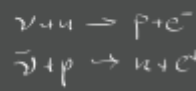
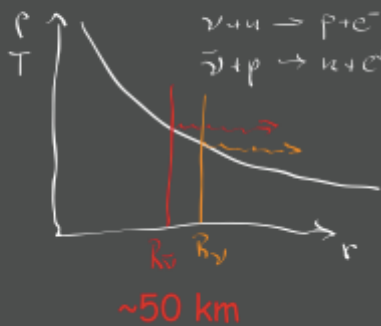


# Neutrino Luminosities

The neutrino luminosities reflect the accretion rate and the thermodynamic conditions at the **neutrinospheres**



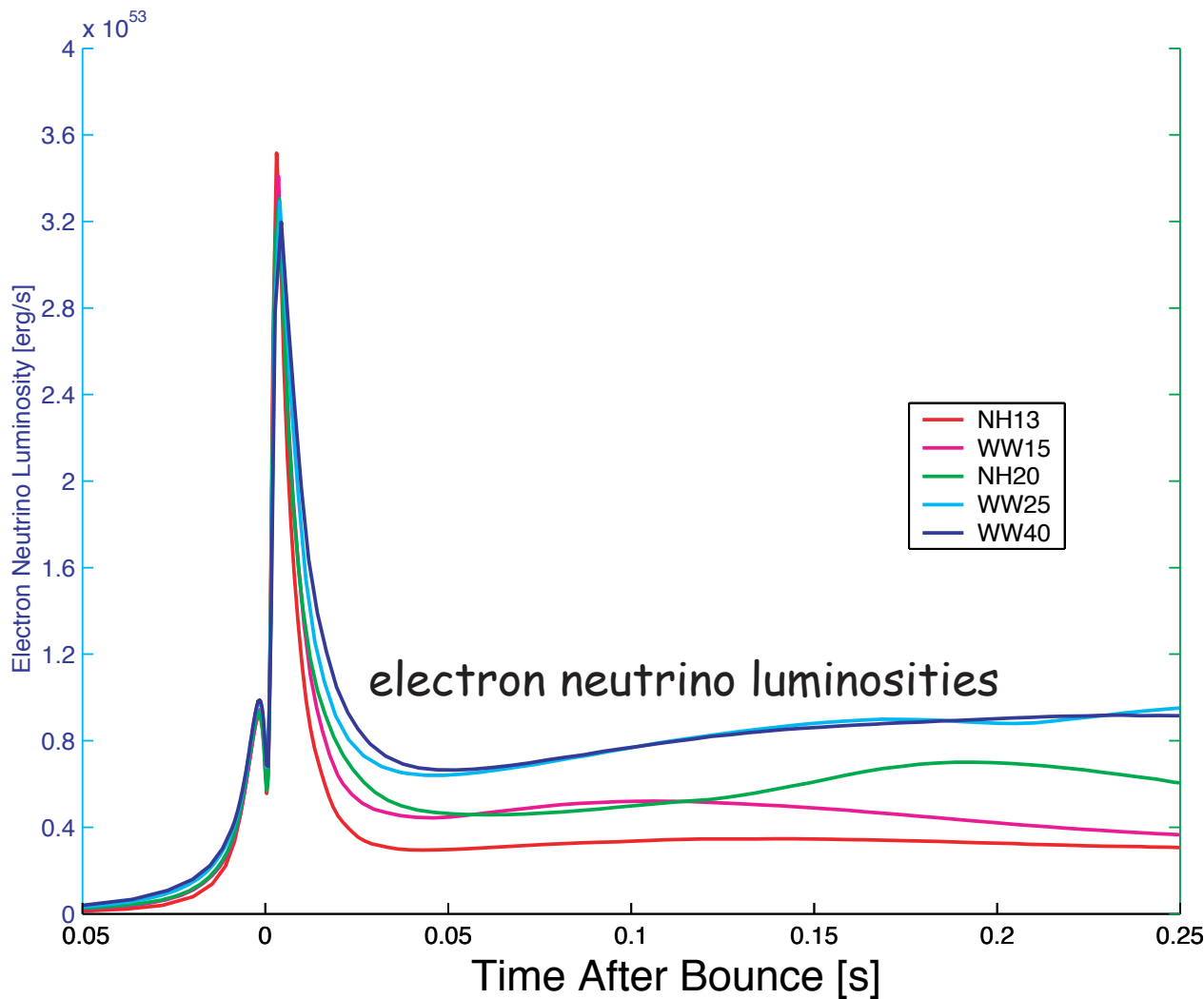
Typical energy hierarchy of neutrino energies:



neutron rich  
 $n_n > n_p$

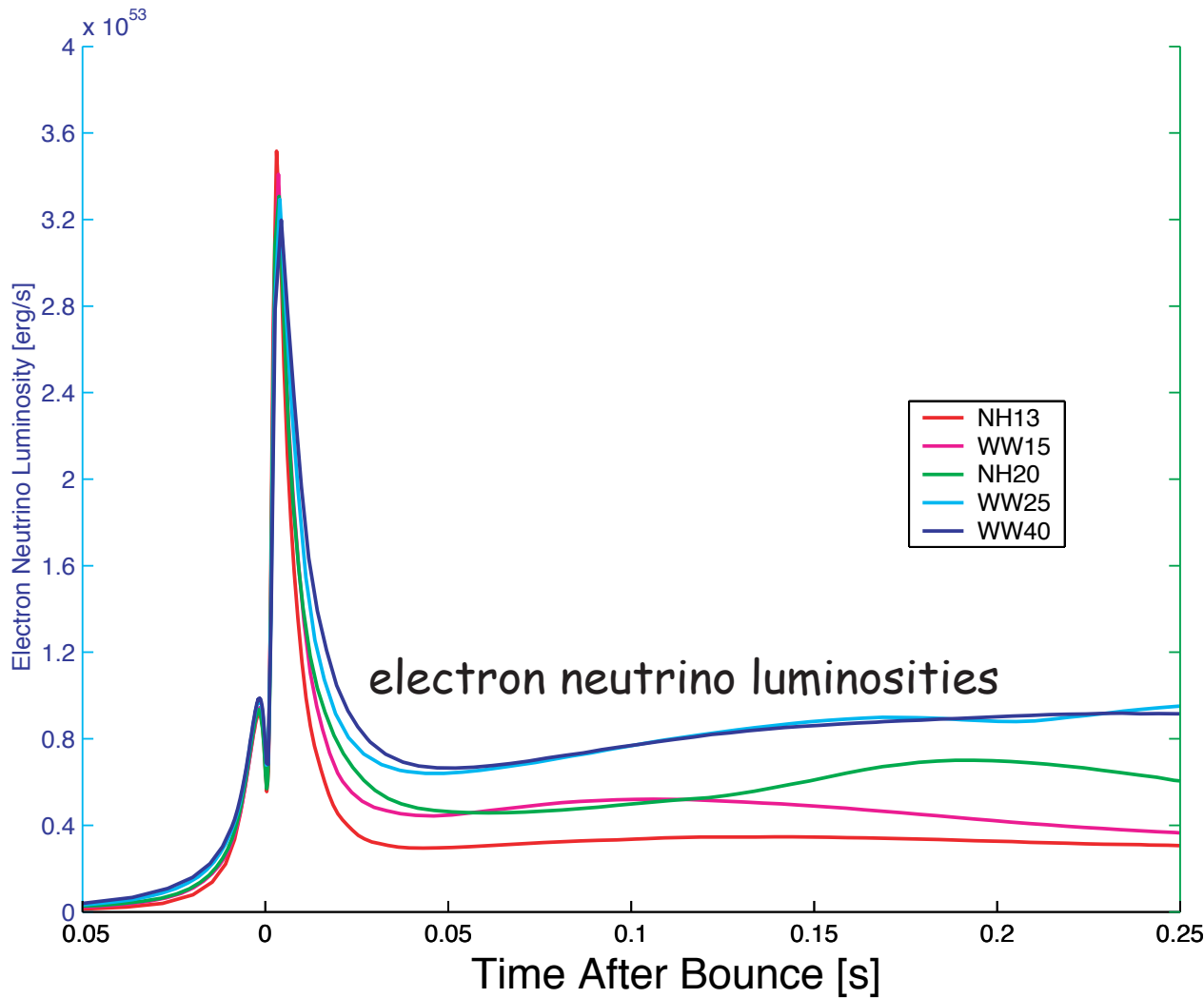
$$\Rightarrow E_{\bar{\nu}} > E_\nu$$

# Neutrino signal

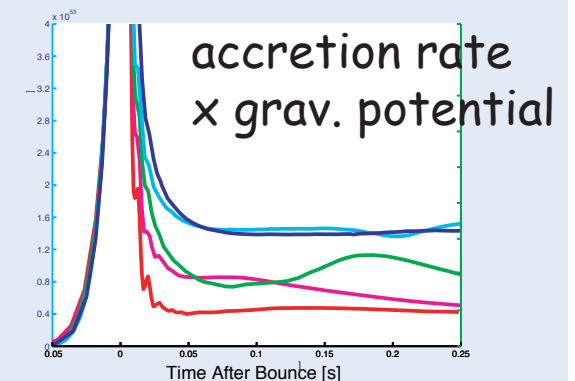


- initially similar luminosities
- differences appear in accretion phase
- >50% accretion lumin.
- density profiles in outer progenitor layers very different

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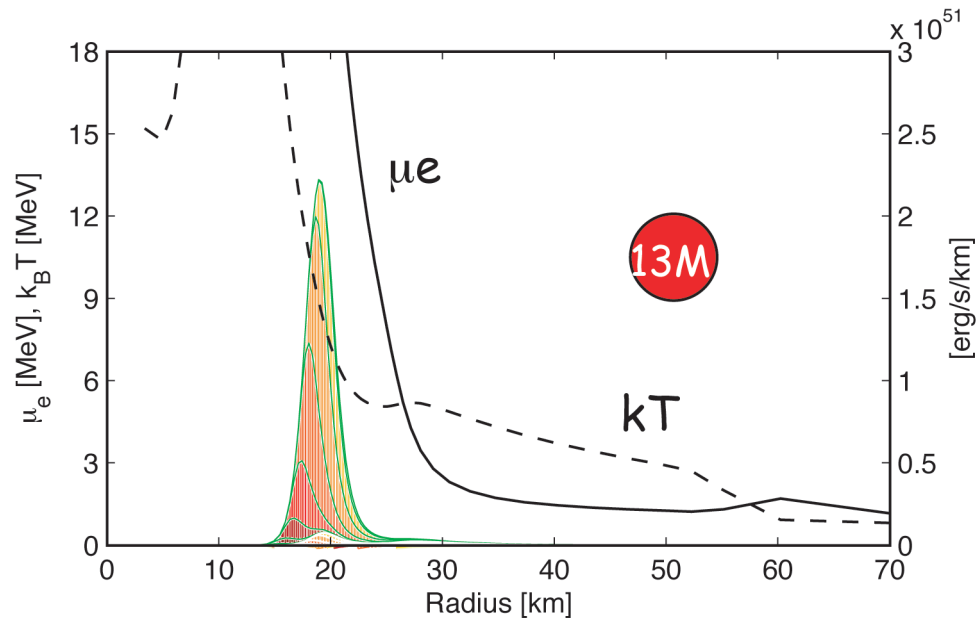


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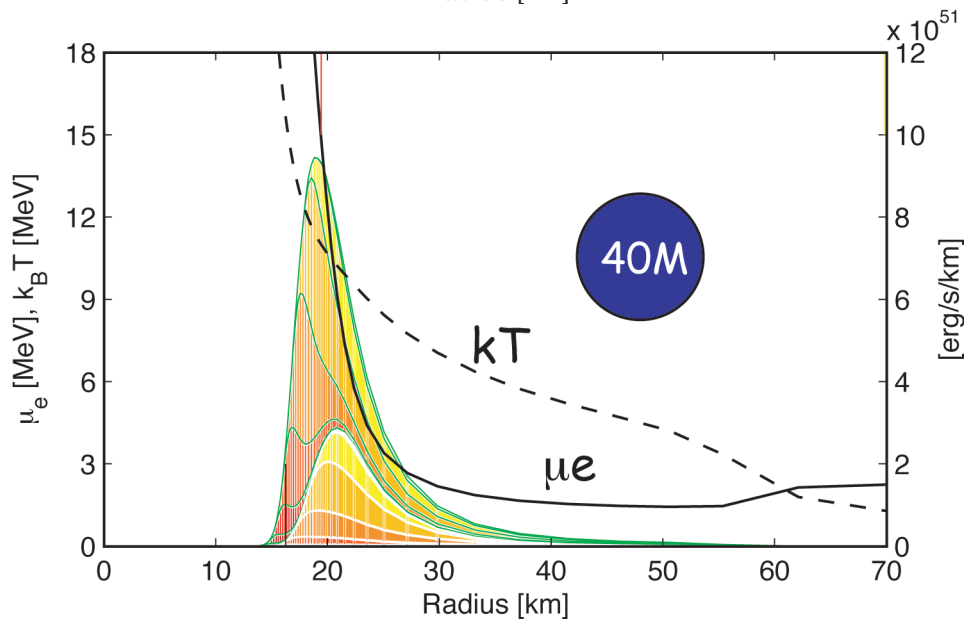
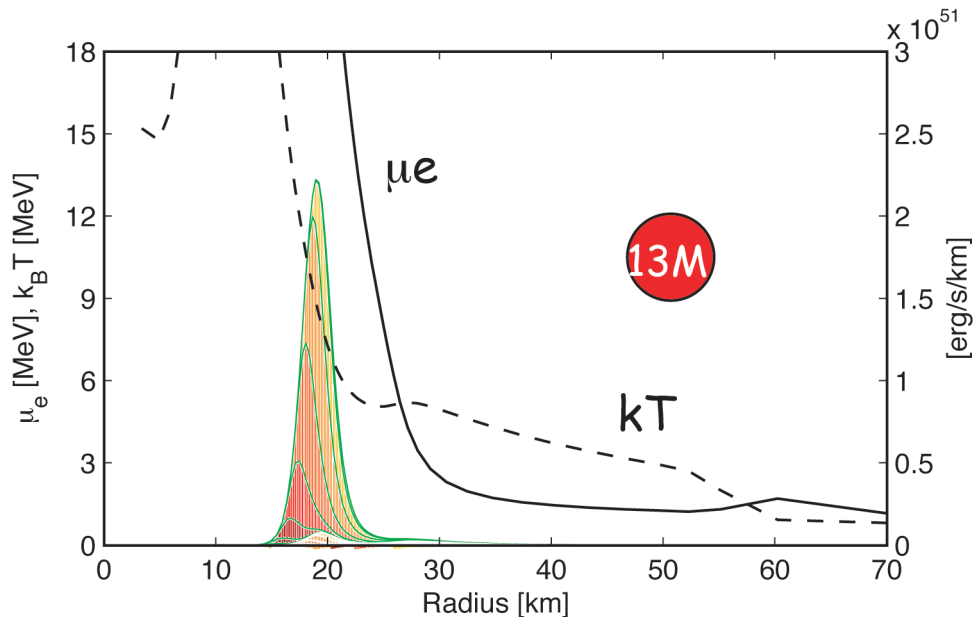


# PNS evolution & $\nu(\mu/\tau)$ properties



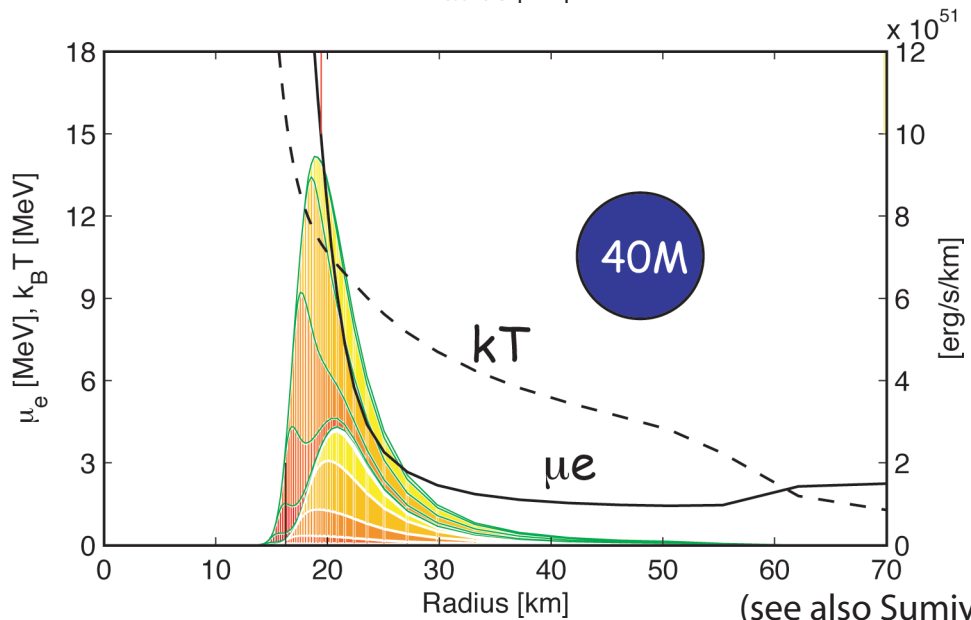
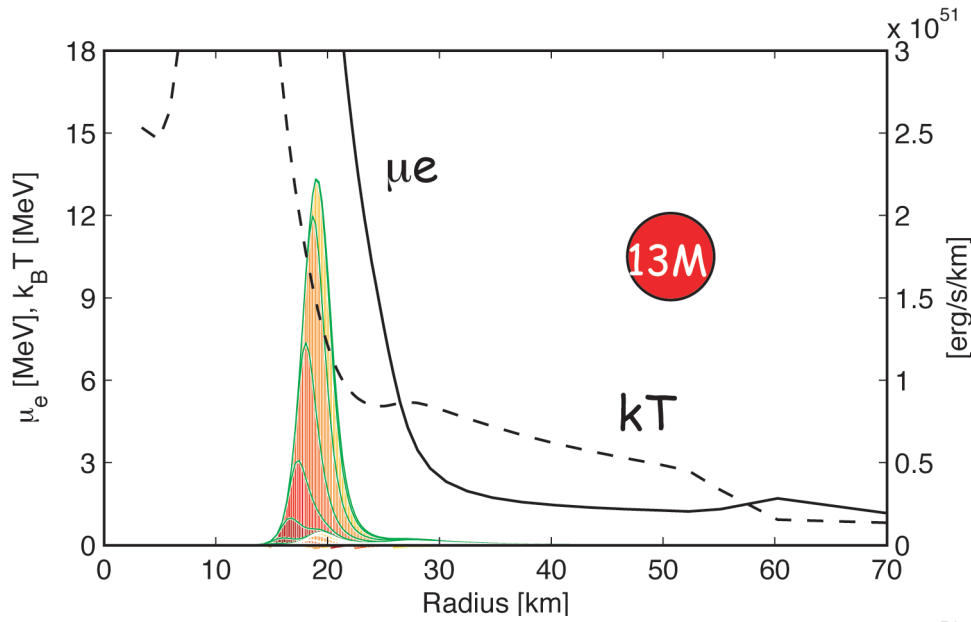
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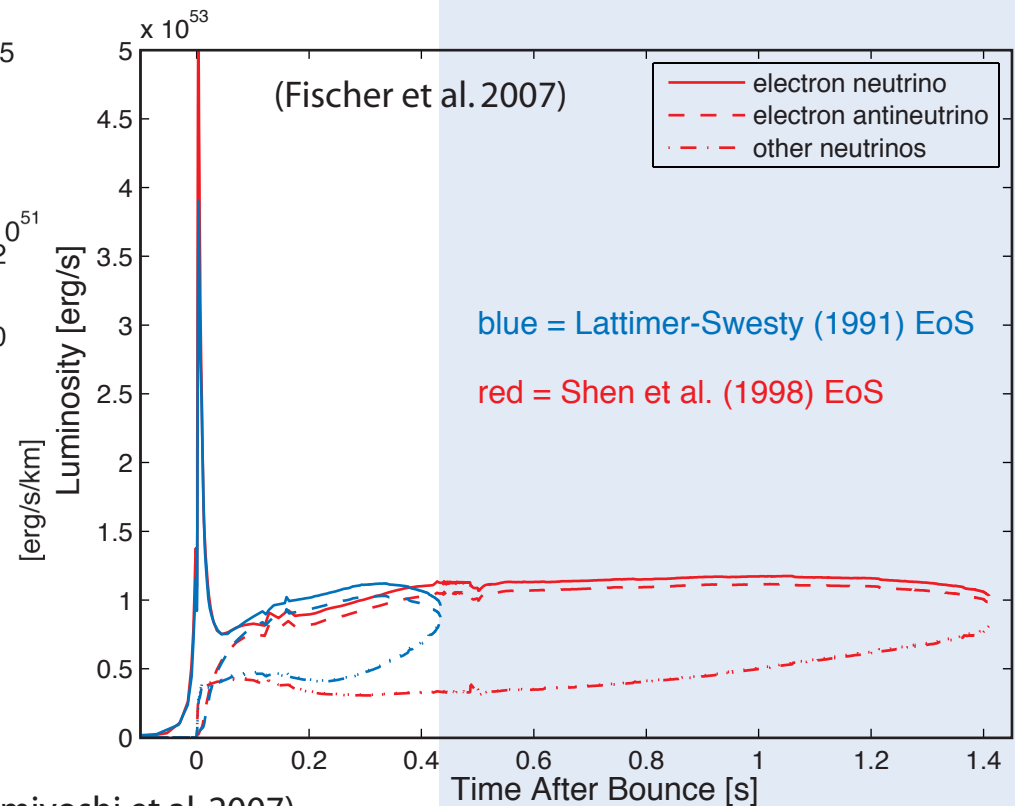


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- PNS close to maximum mass  
--> hot layers pushed inward

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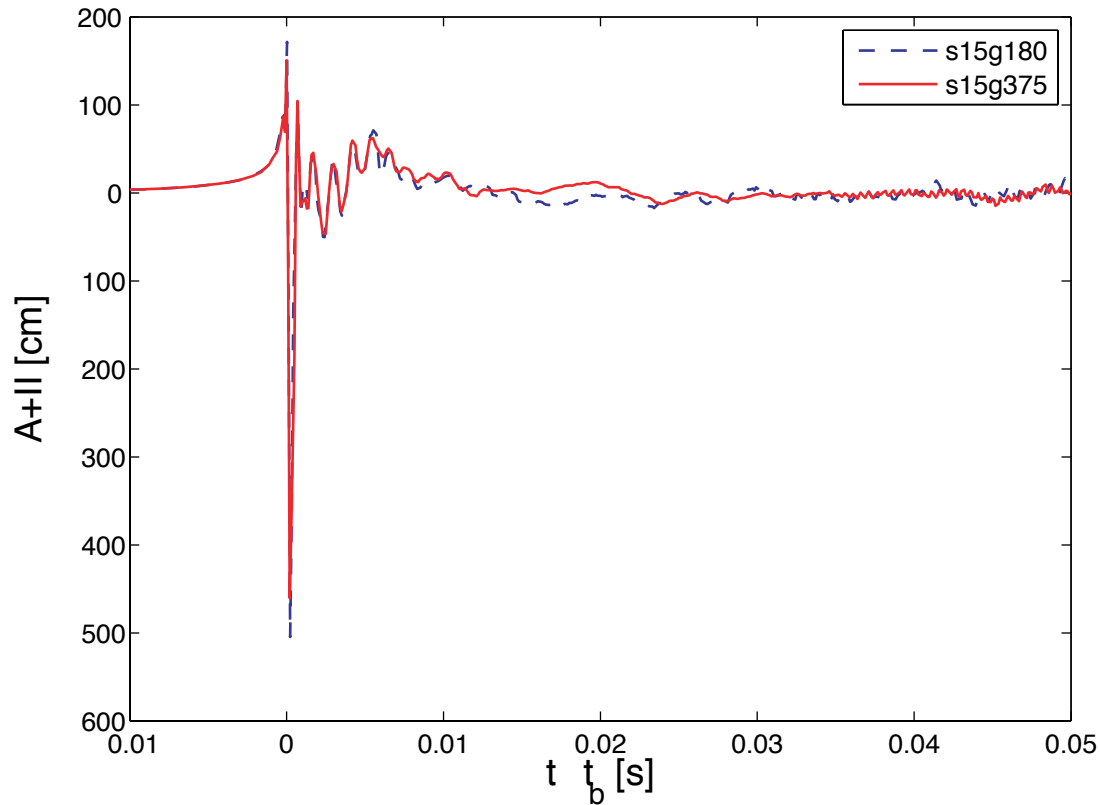


- low mass proto-neutron star (PNS)  
--> incompressible accretion
- PNS close to maximum mass  
--> hot layers pushed inward



(see also Sumiyoshi et al. 2007)

# Testing equation of state at bounce?



- the direct impact is small!
- Is there an indirect impact on fluid instabilities that produce larger variations in GW emission?
- GW from QCD phase transition? (e.g. Yasutake et al. 2007, Abdikamalov et al. 2007)

Run1 -->  $K=180$  MeV

Run2 -->  $K=375$  MeV

Maximum density:

Run1 -->  $\rho=3.8E14$  g/cm<sup>3</sup>

Run2 -->  $\rho=3.6E14$  g/cm<sup>3</sup>

Maximum Amplitude  
(A+II at bounce):

Run1 -->  $A=506$  cm

Run2 -->  $A=406$  cm

Characteristic  
frequency:

Run1 -->  $f_c = 657$  Hz

Run2 -->  $f_c = 565$  Hz

# Influence of Equation of State



## Dynamics/Structure

binding energy per baryon  
--> different temperature  
--> different pressure  
--> different composition -->

## Compositional

different constituents  
--> different neutrino-matter interactions  
--> different freeze-out?  
--> different fragmentation -->

## Microscopic Structure

different arrangements of scattering centers  
--> different coherence effects in neutrino-matter interactions  
--> different binding energy? -->

## References:

(e.g. Baron et al. 1985, Bruenn 1989, Martinez-P., Liebend., Frekers 2006, Sumiyoshi et al. 2005, Marek and Janka 2007, Fischer et al. 2007)

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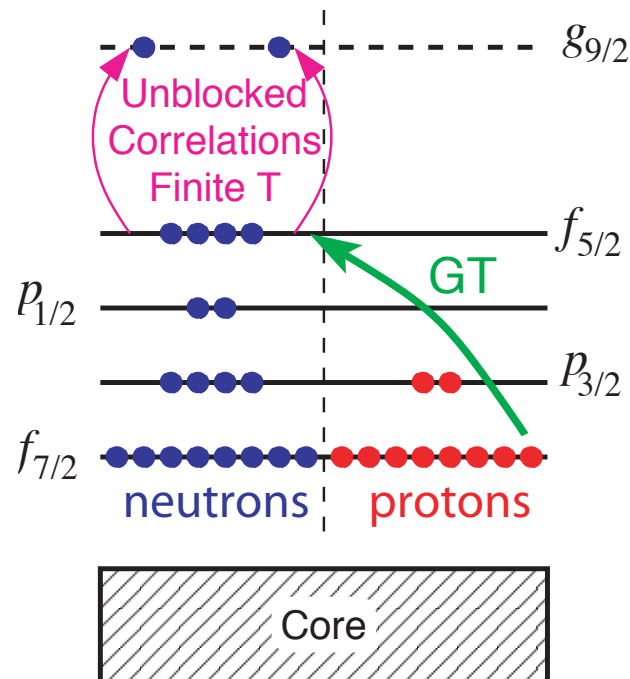
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# Influence of Equation of State

## Dynamics/Structure

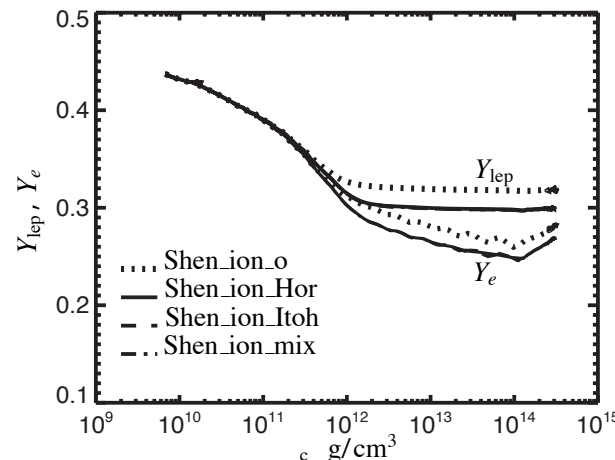
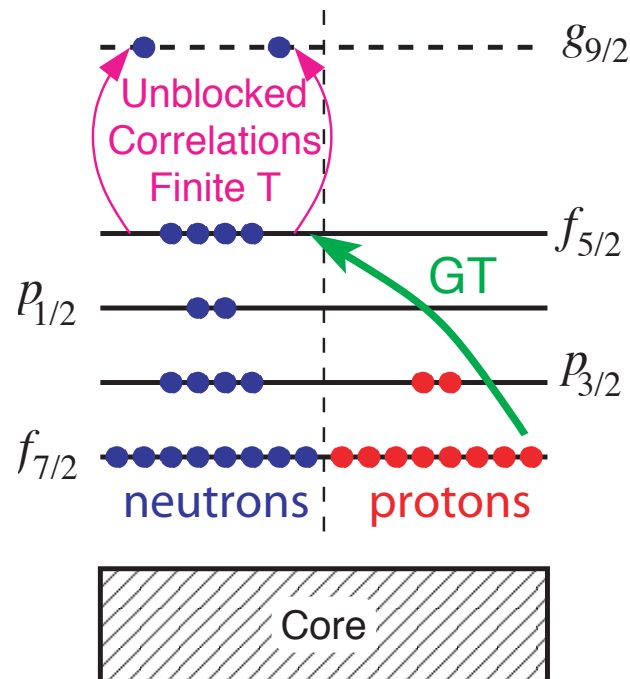
binding energy per baryon  
 --> different temperature  
 --> different pressure  
 --> different composition -->

## Compositional

different constituents  
 --> different neutrino-matter interactions  
 --> different freeze-out?  
 --> different fragmentation -->

## Microscopic Structure

different arrangements of scattering centers  
 --> different coherence effects in neutrino-matter interactions  
 --> different binding energy? -->



## References:

(e.g. Baron et al. 1985, Bruenn 1989, Martinez-P., Liebend., Frekers 2006, Sumiyoshi et al. 2005, Marek and Janka 2007, Fischer et al. 2007)

(Langanke et al. 2003, Hix et al. 2003, Müller et al. 2007, Pruet et al. 2005, Fröhlich et al 2006 Wanajo 2006)

(Itoh 1975, Horowitz 1997, Bruenn and Mezzacappa 1997, Marek et al. 2005, Watanabe 2004, Horowitz et al. 2004, Botvina and Mishustin 2005)